POWER SYSTEM FREQUENCY ESTIMATION ALGORITHM FOR ELECTRIC ENERGY METERING OF NONLINEAR LOADS

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Abstract
In this paper, a discrete wavelet transform (DWT) based approach is proposed for power system frequency estimation. Unlike the existing frequency estimators mainly used for power system monitoring and control, the proposed approach is developed for fundamental frequency estimation in the field of energy metering of nonlinear loads. The characteristics of a nonlinear load is that the power signal is heavily distorted, composed of harmonics, inter-harmonics and corrupted by noise. The main idea is to predetermine a series of frequency points, and the mean value of two frequency points nearest to the power system frequency is accepted as the approximate solution. Firstly the input signal is modulated with a series of modulating signals, whose frequencies are those frequency points. Then the modulated signals are decomposed into individual frequency bands using DWT, and differences between the maximum and minimum wavelet coefficients in the lowest frequency band are calculated. Similarities among power system frequency and those frequency points are judged by the differences. Simulation results have proven high immunity to noise, harmonic and inter-harmonic interferences. The proposed method is applicable for real-time power system frequency estimation for electric energy measurement of nonlinear loads.

Keywords: frequency estimation, power systems, wavelet transforms.

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1. Introduction

In recent years, the electric energy metering for nonlinear loads has drawn the attention of many researchers. For nonlinear loads, the total active power $P$ can be described by (1), where fundamental active power $P_1$ and harmonic active power $P_H$ are given by (2) and (3) respectively.

$$P = \frac{1}{T} \int_0^T u(t) i(t) dt = P_1 + P_H,$$

$$P_1 = V_i I_i \cos \theta_i,$$

$$P_H = \sum_{h>1} V_h I_h \cos \theta_h.$$

The standard IEEE1459-2000 [1] proposed that, for nonlinear loads, $P_H$ and $P_1$ are separately metered, which helps to share power quality responsibility fairly between the consumer(s) and the electric power distributor [2]. To measure $P_1$ and $P_H$, the fundamental frequency $f_1$ needs to be measured firstly. However, the voltage signal collected for frequency estimation is usually composed of harmonics, inter-harmonics, and dc offset, due to the impact of nonlinear loads [3-5]. Moreover, almost all electrical devices are virtually sources of electromagnetic interference. The voltage signal is unavoidably corrupted by noise during measurement and transmits periods. The paper [6] studied the intensity and behavior of noise...
in low-voltage distribution systems. Therefore, for electric energy measurement of nonlinear loads, the frequency estimator should be able to estimate the fundamental frequency \( f_1 \) accurately when the input signal is heavily distorted by harmonics, inter-harmonics, noise etc. Take an energy meter of accuracy class 0.2 for example. The maximum error limit in energy registration is 0.2\%, so the accuracy of fundamental frequency should be improved by two grades, i.e. class 0.05, and it means that the maximum allowable frequency error is 25 mHz for a 50 Hz power system.

In the past several decades, a variety of algorithms [7-26] for frequency estimation have been reported. Generally, the performance of a frequency estimation algorithm can be evaluated through static and dynamic tests. Static tests study the effects of harmonics or noise on the frequency estimator, and dynamic tests study the frequency-tracking performance. These existing algorithms are mainly used for power system monitoring, control and protection. When the power system frequency changes sharply, it will severely endanger the survival of a power system. Therefore these algorithms aim to track fast variations of frequency, and frequency tracking ability is more important than its accuracy and noise-immunity. However, in the fields of energy metering of nonlinear loads, accuracy and noise-immunity of the frequency estimator are especially emphasized, in addition to its frequency-tracking ability.

The modified zero-crossing method [7] and the modified Least Error Squares (LES) algorithm [8] have improved harmonic-resistant performance compared to their original versions. However, those methods still have somewhat poor noise performance. The Kalman filter-based technique includes the extended Kalman filter method [9], extended complex Kalman filter method [10] and robust complex Kalman filter [11]. Researchers try to improve the speed of convergence for frequency estimation, reduce the effects of the neglected high-order terms in Taylor’s expansion, and enhance sensitivity and reliability for detecting a distorted signal. Those algorithms, including the discrete Fourier transforms method [12], transforming discrete Fourier transforms method [13], and Prony’s method [14, 15], suffer from inaccuracies due to more violent fluctuations in the measured signal [11]. The paper [16] introduced an orthogonal FIR-filter-based frequency estimator, which has two averaging filters at the input and the output respectively. The input filter aims to reduce the effects of the 2\(^{nd}\)-order and higher order harmonics. Similarly, the paper [17] studied an adaptive varying step-size Least Mean Square (LMS) method to improve immunity against noise disturbance. The proposed algorithm adopted a third-order Butterworth pre-filter with a crossover frequency of 200Hz to eliminate the effects of harmonics. For these algorithms in [16] and [17] it is a difficult task to design a filter to filter out the inter-harmonic component near to the fundamental frequency without degrading the algorithm’s performance. The phase lock loop (PLL)-based method was proposed in [18] and compared with the adaptive notch filter (ANF)-based method in [19]. Comparison results show that the ANF-based method has better frequency-tracking performance; however, its harmonic (or noise) immunity is worse. In [20], the author introduced a least-squares method. The main characteristic of this algorithm is its short response time; however, its noise-immunity or harmonic-resistant ability is worse than that of the PLL-based method. The demodulation-based methods [21, 22] used two modulating signals. The signal components in the modulated signals, which carry the information of fundamental phase and also around DC, are filtered out by the low-pass filter and used for estimation of phase angle and frequency. The inter-harmonic component near the fundamental frequency, however, is still difficult to be filtered out. Other algorithms, such as the modified LMS algorithm [23], the least mean phase (LMP) algorithm [24] and the multi-harmonic least-squares fitting algorithm [25] are also reported. Reference [26] presents reviews of the existing several methods, outlining strengths and weaknesses of each one.
In power systems, the fundamental frequency usually deviates from its nominal value (50Hz or 60Hz), due to unbalance between generators and consumption or power fault [27, 28]. According to the standard EN50160 [29], the 10-second mean value of the fundamental frequency should be within 49.5–50.5 Hz during 99.5% of a year. Sergei S. Smirnov [30] pointed out that, according to European requirements [31], the average 10-minute frequency deviations should be within a ±20 mHz range. And, based on field measurement, he reported that in Russia’s power systems the fundamental frequency variation was in the range ±10 mHz and the maximum deviation amounts to ±50 mHz, with the averaging 10-minute period. Normally the rate of frequency variation was ±10 mHz/min (about 1.7e-4Hz/s) and may reach ±25mHz/min. (about 4.2e-4Hz/s). It can be observed from Figs [28, 32, 33] (Fig. 7 in [28], Fig. 6 in [32], Fig. 2.6 in [33]) that the rate of frequency fluctuation was normally about less than 20mHz/s under normal operating conditions. According to the above descriptions, the frequency estimator used in the field of power measurement of a nonlinear load should be able to track the slowly-changing frequency.

Wavelet transform is one of time-frequency techniques and has been applied in a wide variety of research areas such as transient analysis, harmonic analysis and power quality monitoring [34-38]. Wavelets are oscillating waveforms with zero mean and start out at zero, increase and then decrease, which have zero amplitude at both ends. The basic idea underlying wavelet analysis involves expressing a section of a signal as a linear combination of a particular set of wavelet functions, and the coefficients represent how closely the wavelet function correlates with the signal in that section. These wavelet functions are obtained by shifting and dilating a mother wavelet. The discrete wavelet transform (DWT), as the digital representation of the continuous wavelet transform, decomposes a signal into different frequency components, and provides a logarithmic division of the frequency domain.

In this paper, the authors introduced a DWT-based approach to power frequency estimation. Similar with the methods [21, 22], the proposed method in this paper is also demodulation-based, using modulating signals \(\sin(2\pi ft)\cos(2\pi ft)\) and \(\sin(2\pi ft)+\cos(2\pi ft)\). The difference between these two methods is that this approach is based on multi-level DWT. Estimation of fundamental frequency is achieved using wavelet coefficients in the lowest frequency band.

The multi-level DWT is implemented using a multistage filter bank with the wavelet function as the low-pass (LP) filter and its dual as the high-pass (HP) filter. Outputs of the LP filters are down-sampled by two for the next stage. To achieve Mallat’s fast algorithm [34], the chosen mother wavelet should be orthogonal (or biorthogonal) and compactly supported. Among the commonly-used wavelets, wavelets that meet these requirements include Daubechies, Coiflets, Symlets and biorthogonal families. In comparison with a classical low-pass filter and a decimator that are used in most publications dealing with demodulation methods, the use of the discrete wavelet transform makes this algorithm show strong harmonic-resistance and noise-immunity. Here the ‘harmonic’ includes odd- and even-order harmonics, inter-harmonics, and sub-harmonics.

The paper is organized as follows. The concept of the proposed frequency estimator is explained in Section II. Section III evaluates the estimator performance under various conditions. Discussions about the proposed estimator are present in Section IV. Section V summarizes the main conclusions of the paper.

2. The proposed algorithm

In this section, the DWT-based algorithm for frequency estimation under nonlinear loads is introduced. The proposed frequency estimator employs \(N\) successive samples within a 0.2 second period (10 times the fundamental period for a 50 Hz system) to estimate the power
system frequency. Suppose the power signal (voltage signal or current signal) is band-limited such that a frequency component at or above 1500 Hz can be neglected. According to the Nyquist-Shannon sampling theorem, a 3200 Hz sampling frequency is chosen. The window size is 0.2 second, and the 640 successive samples within the window are decomposed by DWT at seven levels, and there are five wavelet coefficients in the lowest frequency band (0-12.5 Hz).

The main idea is as follows. Since the power system frequency $f_i$ usually fluctuates within a narrow frequency range (49.5 - 50.5 Hz for a 50 Hz power system) in normal operation, we can predetermine a series of frequency points within this interval, and find out the nearest frequency point (denoted as $f_a$) and the second nearest frequency point (denoted as $f_b$) by some means. The mean value of $f_a$ and $f_b$ is considered as the approximate evaluation of $f_i$, i.e., $f_i \approx 0.5(f_a+f_b)$. Two problems arise here. The first one is how to set up these frequency points. The second one is how to judge the similarity between these frequency points and $f_i$.

The first problem is easy to solve. When the proposed frequency estimator is initially started, eleven frequency points are 49.5 Hz, 49.6 Hz, ..., 50.4 Hz and 50.5 Hz respectively, equally-spaced in the interval [49.5 Hz, 50.5 Hz]. In the following estimation, the interval is limited within the neighborhood of the previous estimated frequency (denoted as $f_i$), i.e., $[f_i-0.05$ Hz, $f_i+0.05$ Hz]. Choice of 0.05 Hz is based on the following considerations. In the first estimation, the interval between adjacent frequency points is 0.1 Hz. Assume the actual fundamental frequency is between the frequency points 49.9 Hz and 50.0 Hz, and the estimated frequency will be 49.95 Hz. The difference between the actual frequency and its estimated value is less than 0.05 Hz. The modified frequency range is obviously narrower than the initial range and the interval between adjacent frequency points is decreased to 0.01 Hz ($f_i+0.05$ Hz)-($f_i-0.05$ Hz)/10=0.01 Hz. This fact helps to increase estimation accuracy. Meanwhile, modification of the frequency range realizes the frequency-tracking capability when the power system frequency fluctuates.

The second problem is exactly how to find out the frequency points $f_a$ and $f_b$ from these frequency points. A detailed approach is as follows: use these predetermined frequency points as the frequencies of a series of modulating signals, and the power signal is modulated by these modulating signals. Those frequency components in the modulated signals whose frequencies equal the difference between the power system frequency $f_i$ and these frequency points, are separated out using DWT, and the corresponding wavelet coefficients are obtained. Denote the difference between the maximum and minimum coefficients in the lowest frequency band as $D_f$. For each modulated signal, one corresponding $D_f$ value is obtained. The frequency point corresponding to the minimum $D_f$ value is considered as the frequency point nearest to $f_i$, i.e., $f_a$.

Assume the power signal $v(t)$ is represented by:

$$
v(t) = V_f \sin(2\pi f_i t + \theta_j) + \sum_{k=2}^{M} V_k \sin(2\pi f_k t + \theta_k).
$$

Here $f_i$, $V_f$, and $\theta_j$ (or $f_k$, $V_k$ and $\theta_k$) represent the frequency, amplitude and initial phase angle of the fundamental component (or the $h^{th}$ harmonic component) respectively. $f_k$ equals $k f_j$, and $M$ is the highest harmonic order. Generate a modulating signal $a_m(t)$, defined by (5). The frequency $f_m$ is selected from these frequency points.

$$
a_m(t) = \sin(2\pi f_m t) .
$$

Multiply $v(t)$ by $a_m(t)$, the modulated signal $v_m(t)$ is obtained:

$$
v_m(t) = v(t) a_m(t) = \sum_{k=1}^{M} V_k \sin(2\pi f_k t + \theta_k) \sin(2\pi f_m t),
$$
where

\[
\sin(2\pi f_t t + \theta_k) \sin(2\pi f_m t) = \frac{1}{2} \cos[2\pi(f_k - f_m)t + \theta_k] - \frac{1}{2} \cos[2\pi(f_k + f_m)t + \theta_k].
\]  

(7)

It can be seen from (7) that the frequency components in the signal \(v_d(t)\) can be represented as \((f_k - f_m)\) or \((f_k + f_m)\), and \(k\) varies from one to \(M\). Usually \(f_1\) is in the frequency range of 49.5 to 50.5 Hz, and \(f_m\) also belongs to this range, so the lowest frequency component is \(\Delta f_i = |f_1 - f_m|\), \(\Delta f_i \in [0 \text{ Hz}, 1 \text{ Hz}]\).

Using multi-level DWT, \(v_d(t)\) is decomposed into wavelet coefficients of individual frequency bands. The lowest frequency band is \((0 - W_b)\) Hz, and \(W_b\) is denoted as the frequency band width. To separate out the frequency component \(\Delta f_i\), \(W_b\) should be less than 50 Hz when \(v_d(t)\) is only composed of a fundamental component and integer harmonics. However, if inter-harmonics exist in \(v(t)\), frequency component \([\Delta f_{\text{inter}} - f_m]\) in the signal \(v_d(t)\) may be less than 25 Hz. Here \(\Delta f_{\text{inter}}\) is the inter-harmonic frequency. In such case, \(W_b\) should be further decreased in order to separate out \(\Delta f_i\). In the following evaluation section, \(W_b\) is 12.5 Hz.

After obtaining the wavelet coefficients, \(D_i\) is calculated. Using eleven different frequency points as the frequency \(f_m\) respectively, eleven \(\Delta f_i\) and the corresponding eleven \(D_i\) values are obtained.

Apart from signal \(a_m(t)\), two different modulating signals \(b_m(t)\) and \(c_m(t)\) are also studied, given by (8) and (9).

\[
b_m(t) = \cos(2\pi f_m t).
\]  

(8)

\[
c_m(t) = a_m(t) + b_m(t).
\]  

(9)

Studies show that \(D_i\) has a certain relationship with \(\Delta f_i\), when \(\Delta f_i\) belongs to the interval \([0 \text{ Hz}, 1 \text{ Hz}]\). When the initial phase angle \(\theta_i\) belongs to a certain interval (discussion below), \(D_i\) monotonically grows with the increase in \(\Delta f_i\). This interval is called a monotone interval, or in other words, the corresponding modulating signal is considered to be monotonic in this interval. Fig. 1(a) shows the monotone and non-monotone intervals corresponding to the modulating signals \(a_m(t)\), \(b_m(t)\) and \(c_m(t)\) respectively. It is observed that there are always two or more modulating signals that are monotonic when \(\theta_i\) varies from 0 degrees to 360 degrees with a step of 1 degree, except several narrow intervals. In the monotone interval, the frequency point corresponding to the minimum \(D_i\) is nearest to \(f_1\) among all frequency points.

However, when the initial phase angle \(\theta_i\) values are in those intervals \([(43 - \Delta, 43 + \Delta), [178 - \Delta, 178 + \Delta], [223 - \Delta, 223 + \Delta], [358 - \Delta, 358 + \Delta], 0 < \Delta < 1\) unit (degrees)), only one modulating signal is monotonic. Further research shows that, for those intervals, although in the whole interval \([0 \text{ Hz}, 1 \text{ Hz}]\) of \(\Delta f_i\), a certain modulating signal is not monotonic, there is still a narrower interval in which the signal is monotonic. Furthermore, the \(D_i\) value corresponding to the minimum \(\Delta f_i\) is also the minimum. For example, when the initial angle \(\theta_i\) is 358 degrees, the relationship of \(D_i\) values versus \(\Delta f_i\) is depicted in Fig. 1(b). Here the signal \(a_m(t)\) is monotonic for the whole interval \([0 \text{ Hz}, 1 \text{ Hz}]\), and the non-monotonic intervals for signals \(b_m(t)\) and \(c_m(t)\) are \([0.04 \text{ Hz}, 0.05 \text{ Hz}]\) and \([0.99 \text{ Hz}, 1 \text{ Hz}]\) respectively. So two or more modulating signals are monotonic whatever the frequency deviation is, when the initial phase angle \(\theta_i\) is 358 degrees.
Synthesized from the above descriptions, the following conclusions are obtained. If two or more modulating signals determine the same points nearest to the fundamental frequency \( f_1 \), it means that this frequency point is \( f_a \). Meanwhile, these corresponding modulating signals are monotonic.

After the point \( f_a \) is detected, the next step is to find out the second-nearest frequency point \( f_b \). There are two frequency points nearest to \( f_a \) among all frequency points, one on the left side (denoted as \( f_b_1 \)) and the other on the right side (denoted as \( f_b_2 \)). When the modulating signal is in the monotone interval, the frequency point corresponding to the smaller \( D_f \) value is \( f_b \). For example, if the frequency point \( f_a \) is 49.7 Hz, co-determined by the signals \( a_m(t) \) and \( b_m(t) \), the two frequency points nearest to \( f_a \) are 49.6 Hz and 49.8 Hz respectively. According to the previously mentioned description, the signals \( a_m(t) \) and \( b_m(t) \) are both in the monotone interval. Select one of the two signals arbitrarily, for example, \( a_m(t) \). For signal \( a_m(t) \), if the \( D_f \) value of the right point (49.8 Hz) is smaller than that of the left point (49.6 Hz), \( f_b \) is 49.8 Hz.

According to the linearity of discrete wavelet transform [39, 40], (10) exists, where \( DWT(\cdot) \) means the discrete wavelet transform operator. Equation (10) shows that the wavelet coefficients of signal \( c_m(t) \) can be directly calculated from those of signals \( a_m(t) \) and \( b_m(t) \), and therefore calculation complexity is reduced.

\[
DWT(c_m(t)) = DWT(a_m(t)) + DWT(b_m(t)).
\]  

3. Evaluation of the proposed algorithm

The performance of the DWT-based frequency estimator proposed in this paper has been evaluated under static and dynamic conditions using computer simulation. In the static tests, the effects of noise, harmonics, inter-harmonics and dc offset are evaluated. In the dynamic tests, the capability of the frequency estimator in tracking step, ramp, and oscillatory variations of frequency is evaluated. Effects of amplitude and phase jumps in the power signal are also studied. The evaluation is compared with the PLL-based method [18] and the ANF-based method [19]. Finally the voltage samples collected from the power system are analyzed by the proposed algorithm. Here the sampling frequency is 3200 Hz, the wavelet function is db5, and the window size is 0.2 second (640 samples). Seven-level DWT is performed to obtain the wavelet coefficients in the frequency band (0-12.5 Hz). Similar results are obtained when other wavelet functions (wavelets that belong to Daubechies, or Coiflets, or Symlets or biorthogonal families) are used, and are not shown here for simplification.
3.1. Static test

3.1.1. Noise

The test signal is a pure sinusoidal signal with unity amplitude, corrupted with zero-mean Gaussian white noise. Fig. 2 (a) shows maximum errors of the proposed algorithm, the ANF-based method and the PLL-based method, when the signal-to-noise ratio (SNR) varies from 20dB to 60dB. It is observed that the noise immunity feature of the proposed algorithm is desirable, and competes with that of the ANF-based method. However, the proposed frequency estimator provides less-accurate responses compared with the PLL-method, when noise is present.

3.1.2. Harmonics and DC Component

To study the impact of harmonics and DC offset on the performance of the frequency estimator, several examples are considered, where the input signal is a fundamental component plus DC offset, or a fundamental component plus a third harmonic, or a fundamental component plus a fifth harmonic, or composed of a fundamental component, DC offset and harmonics (2\textsuperscript{nd} ~ 25\textsuperscript{th}). The estimated frequency has a fixed error (5 mHz) when the relative magnitude of DC offset or a single harmonic component with respect to that of the fundamental component varies from 0% to 50%. This study shows that the impact of DC offset or harmonics is negligible. For the ANF-based method or the PLL-based method, the estimated frequency is subject to an oscillatory steady-state error and an offset error. The maximum error equals the sum of the oscillatory and offset errors due to individual harmonic components. For example, when the test signal is composed of a fundamental and the 3\textsuperscript{rd} harmonic component, the maximum errors of these frequency estimators are illustrated in Fig. 2 (b).

It is observed that the performance of the proposed algorithm is better, compared with the ANF based method. In the case of low harmonic distortion level, the performance of the PLL-based method competes with the proposed method. However, when the harmonic distortion level increases, the proposed method outperforms the PLL-based method. Meanwhile, the PLL-based method uses a second-order band-pass pre-filter to reduce the effects of harmonics, and the cutoff frequencies are 10 Hz and 110 Hz. Obviously, an inter-harmonic frequency component near to the fundamental frequency is difficult to be filtered off by this filter. And the task to design such a filter without degrading the performance of the frequency estimator is difficult to achieve.

3.1.3. Inter-harmonics

The test signal is composed of a fundamental component with unity amplitude and an inter-harmonic component. Three cases with different inter-harmonic amplitude (0.01 p.u, 0.02 p.u, and 0.05 p.u) are studied. When the inter-harmonic frequency varies from 15 Hz to 48 Hz, the maximum estimation error of the proposed estimator is depicted in Fig. 2 (c). It is observed that the estimation error depends on the inter-harmonic frequency and amplitude. For example, when the input signal is composed of a fundamental component and the inter-harmonic component (frequency: 40 Hz, amplitude: 0.05), the error is less than 35 mHz. This study shows that the proposed algorithm has a strong inter-harmonic immunity.
3.2. Dynamic test

3.2.1. Jumps in Amplitude or Phase Angle

Switching may cause a step change in voltage amplitude or phase in power systems [41]. The impact of such step changes on the performance of the frequency estimator should be as small as possible. Simulation results show that step changes in the amplitude or phase angle result in no steady-state errors in the estimated frequency when the amplitude or phase of the input signal undergoes a jump of 0.5 pu (amplitude) or 60 degrees (phase). However, a transient error of 50 mHz is observed when the phase angle of the input signal jumps. For the PLL-based method or ANF-based method, step changes in the amplitude or phase angle also result in no steady-state errors in the estimated frequency. For the ANF-based method, the transient error is 200 mHz for an amplitude step, and 3 Hz for a phase angle step. For the ANF-based method, the transient error is 800 mHz for an amplitude step, and 1.5 Hz for a phase angle step. The drawback of the proposed frequency estimator is that its transient time is 0.2 second, longer than that of the PLL-based method (about 0.1s) or that of the ANF-based method (about 0.08s).

3.2.2. Oscillatory Variations of Amplitude

The impact of oscillatory variations of amplitude on the estimated frequency is studied. When the amplitude of the input signal changes from its nominal value of 1 to 1+0.2\(\sin\pi t\), the maximum error of the estimated frequency is 5 mHz, less than 20 mHz of the ANF-based method.

The following section is devoted to verify the performance of the proposed frequency estimator in tracking various types of frequency variations, including ramp, step and oscillation. However, the proposed frequency estimator is used for a power energy meter. Therefore, different from those in [18] and [19], only frequency variations whose frequency-rate-of-change (df/dt) is less than 0.2 Hz/second or a single step-change is less than 0.2 Hz, are studied.
3.2.3. Ramp Variations of Frequency

The capability of the proposed method in tracking ramp variations of frequency is depicted in Fig. 3. The frequency-rate-of-change of the input signal is 0.1Hz/second. The true frequency and its estimated value are shown in Fig. 3(a), and the estimation error is shown in Fig. 3(b). This study shows that the estimated frequency faithfully follows the true ramp with a delay of 0.2 seconds.

![Fig. 3. Frequency tracking for ramp variation (a) frequency variation curves (b) the estimation error.](image)

3.2.3. Oscillatory Variations of Frequency

The paper [41] pointed out that the power system frequency can fluctuate due to electromechanical oscillations of generators. An example is considered to illustrate the performance of the proposed estimator with respect to oscillatory frequency variations. The frequency of the input signal is \( f(=50+\sin 0.04\pi t) \). The maximum rate of change of frequency is \( 0.04\pi \text{Hz/s} (<0.2\text{Hz/s}) \). The actual frequency and its value estimated by the proposed estimator are shown in Fig. 4(a). It is observed that the estimated frequency follows the actual frequency with a delay of 200ms. Fig. 4(b) shows the estimation error. This study shows that the proposed frequency estimator can track frequency oscillatory variations when the rate of change of frequency is small.

![Fig. 4. Frequency tracking for oscillatory variation (a) frequency variation curves (b) the estimation error.](image)
3.2.4. Step Variations of Frequency

Here the frequency of the input signal makes a step change at 2.7174 s. The actual frequency and its estimated values by the proposed estimator are shown in Fig. 5. Three cases with different step changes of 50 mHz, 100 mHz and 200 mHz are considered, and the corresponding results are illustrated in Fig. 5 (a), (b), and (c) respectively. It is observed that the steady-state error is 10 mHz no matter whatever the step change is; however, the transient time grows with an increase of the step change. It is so because the modification of the frequency estimation range takes more much time for a large step change. The response time of the proposed method is less than 600 ms for a step change of 50 mHz (or 100 mHz), and less than 1000 ms for a step change of 200 mHz.

3.3. Frequency estimation using a real voltage signal from the power system

The voltage signal from the power system is adjusted by a voltage adjustor, and then through a converter (100V/4V), is finally collected by a NI6221 data acquisition card (National Instrument, 16-bit A/D converter). The collected signals are analyzed by the proposed algorithm, and the fluctuation curve of power system frequency is illustrated in Fig. 6. As the true frequency of the power system was not known, estimation errors cannot be calculated. However, the estimation quality of the proposed algorithm can be judged from their consistency [13, 16]. The maximum variation in the measured frequency is about ±0.04Hz. This demonstrates the effectiveness of the proposed algorithm for power system frequency estimation.

Fig. 5. Frequency tracking for step variations (a) 0.05 Hz step change (b) 0.1 Hz step change (c) 0.2 Hz step change.

Fig. 6. Frequency measurement results of a voltage signal taken from the grid.
4. Discussions

The proposed estimator employs \( N \) successive samples within 10 times the nominal fundamental period (0.2 second for a 50 Hz power system). These samples are decomposed by multi-level DWT to obtain the wavelet coefficients in the lowest frequency band which are used to estimate the power system frequency. \( N \) equals \( 0.2f_s \), and \( f_s \) is the sampling frequency. Here some important parameters, including window size, decomposition level, sampling frequency and choice of wavelet function are needed to be further explained.

The sampling frequency \( f_s \) is selected to be \( 2^r \) times the nominal fundamental frequency and \( r \) is an integer. Also \( f_s \) should be higher than two times the harmonic frequency to meet the requirements of the Nyquist-Shannon sampling theorem. Usually frequency components higher than 1600 Hz are negligible, so the sampling frequency of 3200 Hz is an appropriate choice.

Here the choice of window size is based on the following considerations, in addition to the requirements of the standard [42]. If the window size is 5 times the nominal fundamental period, \( N \) equals \( 0.1f_s \). For multi-level DWT decomposition, assume the decomposition level is \( h \), the number of wavelet coefficients (denoted as \( M \)) in the lowest frequency band will be \( N/(2^h) \), and \( M \) should be an integer. When \( N \) equals \( 0.1f_s \), the maximum decomposition level is 5 (\( f_s = 1600 \) Hz) or 6 (\( f_s = 3200 \) Hz), and the lowest frequency band is (0 Hz-25 Hz). When \( N \) equals \( 0.2s \), the maximum decomposition level is 6 (\( f_s = 1600 \) Hz) or 7 (\( f_s = 3200 \) Hz), and the corresponding lowest frequency band is (0 Hz-12.5 Hz). \( W_b \) is 12.5 Hz. As described in section II, the decrease of the lowest frequency bandwidth will help reduce the effects of inter-harmonics. So the window size is usually set to be 0.2s (for a 50 Hz system). According to the characteristics of multi-level DWT, the decomposition level (denoted as \( K \)) is decided by \( f_s \) and \( w_b \), as described in (11). Here \( w_b \) is the width of the frequency band, which usually is selected to 12.5 Hz.

\[
K = \log_2 \left( \frac{f_s}{2w_b} \right).
\]  

(11)

For real-time power metering, the calculation procedure including estimation of the fundamental frequency, harmonic parameters, and calculation of power-related quantities should be done within a 0.2 s period. To simplify verification, the proposed algorithm is initially performed in the MATLAB environment and two commands (tic and toc) are used to make a rough estimation of execution time. It has been found that the execution time increases when the sample number increases or the number of wavelet filter coefficients (denoted as \( N_f \)) increases. Take the Daubechies family for example. \( N_f \) is 10 for Db5, or 20 for Db10, or 40 for Db20. Table 1 demonstrates different execution time when sample number or Db wavelet is different. Only three different wavelet functions (Db5, Db10 and Db20) are present in the table. Here the used computer is HP 540 (CPU: Intel(R) Core(TM) Duo CPU T 5670@ 1.80 GHz, 1.99 GHz). For example, if the sample time is 640 and the Db5 (or Db10) wavelet is used, the corresponding computation time is 97 (or 99) milliseconds. It means that Db5 or Db10 is suitable for real-time application. For further evaluation of computational complexity, implementation of the use of assembly language in the industry control computer will be the future research goal. Furthermore, theoretical analysis of the relationship between \( D_f \) and \( \Delta f_f \) will also be the further work, because it will be helpful to clarify the characteristics of this approach.
Table 1. Execution time of the proposed algorithm (in milliseconds).

<table>
<thead>
<tr>
<th>Wavelet function</th>
<th>Sample number</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>320</td>
</tr>
<tr>
<td>Db 5</td>
<td>59</td>
</tr>
<tr>
<td>Db 10</td>
<td>60</td>
</tr>
<tr>
<td>Db 20</td>
<td>281</td>
</tr>
</tbody>
</table>

5. Conclusions

This paper proposes a DWT-based approach for estimation of power system frequency. The noise immunity of this approach is comparable to that of the ANF-based method, and smaller than that of the PLL-based method. And its harmonic (or inter-harmonic) immunity outperforms those of PLL-based or ANF-based methods. The main drawback is the high computation complexity and the corresponding long computation time. Therefore, the dynamic response of the proposed method with regard to step, ramp, and oscillatory changes of frequency are slower than those of PLL-based or ANF-based methods. Simulation results show that the frequency error of the proposed algorithm is less than 25 mHz in most cases. Furthermore, if the proposed algorithm is implemented in parallel computation, the computation time will be greatly reduced. This approach is suitable for power system frequency estimation for energy metering of a nonlinear load.

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