The study describes the influence of a surface modification in cored, thin-walled castings of blades from IN-713C nickel superalloy on γ′ phase precipitates. The blades were produced by using the investment casting process in the laboratory conditions as parts for a low-pressure turbine rotor. The microstructural observations of the γ′ phase precipitates on the cross sections of the blades were performed. The observations were followed by quantitative metallography evaluation, and finally, a comparison of the precipitates between one blade with the conventionally applied ceramic core and one with the core covered layer contained a surface modifier (5% of CoAl2O4) was made.

**Keywords:** IN 713C, superalloy, γ′ phase, metallography, statistical analysis

1. Introduction

The γ′ (gamma prime), the tiny coherent phase is the key to the superalloy’s high temperature strength. The development of nickel-base superalloys for turbine applications has focused on increasing the volume fraction of the γ′ phase [1]. Cast polycrystalline nickel-base superalloys are typically composed of γ′-phase coherently precipitated in a face-centred cubic (fcc) matrix, together with eutectic phases and one or more carbide phases. The desired properties and resistance to microstructural changes at high temperatures in these alloys are obtained by all phases with a suitable structure, shape, size and distribution. Among all the microstructural factors, the γ′ precipitate morphology plays an important role in influencing the properties of nickel-base superalloys [2]. The mechanical properties of nickel-base superalloys are strongly influenced by the morphology of the strengthening γ′ precipitates [3]. The γ′ precipitates in Ni-based superalloys should be of optimum size, shape and distribution in order to have the desired properties and resist microstructural changes when performing at high temperatures [4]. According to [5], both the sizes and area fractions of different populations of precipitates are influential and therefore need to be quantified and modeled. The investigated material IN713C is the superalloy known since over 40 years. It is still applied for the aircraft parts because its low price and low density comparing to others nickel-based superalloys [6]. The research conducted under the project [7] confirmed the ability of the surface modifier CoAl2O4 application in the superalloy casting for obtaining grain of required size. In this study the impact of the CoAl2O4 on the γ′ phase precipitates was analyzed.

2. Materials and methods

The studied blades were cast in the precision foundry of Pratt and Whitney, Rzeszow, Poland. IN713C is a commercially available, a precipitation hardenable, nickel-chromium base cast alloy [8-10]. It is characterized by good castability and stability and high strength, as well as a high ductility at elevated temperatures. Its good creep resistance, remarkable resistance to oxidation and thermal fatigue, as well as outstanding structural stability enable its use in gas turbines.

Two cross-sections were cut off from the each blade, as shown in Figure 1. Each cross-section for the microstructure observations was cut along the axis of the blade (Fig. 2). As a result, four pieces from each blade were obtained: two pieces with convex surfaces (a pressure side of the airfoil lying close the core marked with M) and two with concave surfaces (a suction side of the airfoil lying close a core marked with B). The influence of the typical ceramic core and the core with the 5% surface modifier on the material of the IN713C superalloy was examined, which is why the surfaces lying close the ceramic cores were observed using a scanning electron microscope Hitachi S-4200 equipped with EDS.

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The microstructure of the investigated eight pieces from two castings produced using two kinds of cores was observed on polished and etched metallographic specimens. The specimens were ground and polished with vibratory polishers used for final polishing. The specimens’ surfaces prepared in this way were etched with a solution containing: 100 ml H₂O, 100 ml HCl, 100 ml HNO₃ and 3 g MoO₃ by immersion.

The studies which were carried out included a selection of acquisition and image registration parameters. In performed observations, the same image magnification was applied for all the samples in order to compare microstructure in the respective cross-sections.

The recorded microphotographs with γ’ phase precipitates were applied for computer-aided image analysis by means of Met-Ilo program [11] to measure and estimate quantitatively the main parameters describing the γ’ phase precipitates.

3. Statistical methods

Three input factors, each at two levels, may be distinguished in the experiment:

- TECH, technology (the traditional core and the covered with the 5% modifier),
- HEIGHT, height (labelled by 1 or 2),
- TRACE, surface (labelled by B or M).

The full factorial two-level experimental design leads to 8 different treatments.

Two quantitative outcomes were measured: AREA (the plane section area of the precipitates) and \( A_{\delta} \) (the area fraction of the precipitates, which is an estimator of their volume fraction).

The analysis started from the fixed-effect model containing linear (main) effects, three two-way interactions and one three-way interaction [12,13].

During the stepwise regression (backward elimination variant) the non-significant terms were eliminated.

The complete results include: the analysis of effects, the Pareto plot of effects, the fixed-effect model and the identification of homogeneous groups of data based on the least significant difference (LSD) test [12]. The conclusion refers to the impact (or the lack of it) induced by the particular input factor.

4. Results

The analyzed material in as-cast state with the application of the traditional core and covered with the 5% modifier contains γ’ phase in the form of precipitates, varying in terms of their size.

![Fig. 1. Scheme of turbine blade with marked cross-sections for research](image1)

![Fig. 2. The way of cutting of cored, thin-walled part of the turbine blade casting](image2)

![Fig. 3. Characteristic γ’ phase precipitates in the IN713C as-cast superalloy in the studied cross-sections with the traditional core and covered with the 5% modifier. SEM, SE](image3)
and morphology. It is confirmed in Fig. 3, where examples of $\gamma'$ phase precipitates at the dendritic cores, within the ($\gamma + \gamma'$) eutectic islands, and at the interdendritic regions were observed.

The quantitative analysis of the $\gamma'$ phase at the analyzed cross-sections of the turbine blades was limited to the examination of cube-shaped precipitates at the dendritic cores as those having more repetitive morphology and size. It was established that there is a visible difference between the size of $\gamma'$ phase precipitates in cross-sections with No. 1 and No. 2 both with the traditional and covered with the 5% modifier core (see Figs. 4 and 5). It is the result of the applied feeding system, which was closer to cross-section with No. 2.

To evaluate if the core with the 5% modifier affects size, shape and volume fraction of the $\gamma'$ phase precipitates performing an image analysis of these precipitates and presenting their description as numerical data is required. The recorded microphotographs with the $\gamma'$ phase precipitates were applied for the computer-aided image analysis by means of Met-Ilo program [11] to estimate quantitatively the main parameters describing the $\gamma'$ phase precipitates. A precise quantitative evaluation of the $\gamma'$ phase precipitates is complicated because of their complex morphology. This requires image processing and analysis methods so as to obtain binary image of the $\gamma'$ phase precipitates for measurement. An example of the $\gamma'$ phase precipitates detection was presented in Fig. 6.

An analysis of the $\gamma'$ phase precipitates was performed by means of traditional quantitative metallography, using image analysis. The analysis of repeatability of the $\gamma'$ phase precipitates was performed in accordance with the typical statistical methodology [12].

The results of measurements of the $\gamma'$ phase precipitates are presented in Table 1.

The maximal error of area fraction ($A_d$) on the basis of the $\delta$ error was estimated. The highest value of the maximal error of area fraction ($A_d$) was 7.57% for the traditional core_2B cross-section. On the grounds of the data in Table 1 we can observe that finer $\gamma'$ phase precipitates (with smaller values of mean plane section area) there are within cross-sections with No. 1 in the case of the both kinds of cores application. Simultaneously, the $\gamma'$ phase precipitates within these cross-sections are characterized by higher number of $\gamma'$ phase precipitates per unit area of plane section, specific length of $\gamma'$ phase precipitates boundaries and specific surface of $\gamma'$ phase precipitates boundaries in comparison to cross-sections with No. 2.
The outcomes were measured at 8 different treatments, each with 2 replications. The analysis of effect revealed that only the HEIGHT factor affects significantly the outcome \( AA \) (see Table 2), which is indicated by \( p < 0.05 \). All other factors have an insignificant impact on the outcome \( AA \).

**TABLE 2**

<table>
<thead>
<tr>
<th>Cross-sections</th>
<th>Parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>( A_4 ) [%]</td>
</tr>
<tr>
<td>--------------------------------</td>
<td>-------------------------</td>
</tr>
<tr>
<td>the 5% modifier _2B</td>
<td>55.83</td>
</tr>
<tr>
<td>the 5% modifier _1M</td>
<td>55.22</td>
</tr>
<tr>
<td>the 5% modifier _1B</td>
<td>50.21</td>
</tr>
<tr>
<td>the 5% modifier _2M</td>
<td>49.70</td>
</tr>
<tr>
<td>the traditional core _1B</td>
<td>53.31</td>
</tr>
<tr>
<td>the traditional core _1M</td>
<td>56.28</td>
</tr>
<tr>
<td>the traditional core _2B</td>
<td>49.69</td>
</tr>
<tr>
<td>the traditional core _2M</td>
<td>51.56</td>
</tr>
</tbody>
</table>

where: \( A_4 \) – area fraction, \( A \) – mean plane section area, \( v(\bar{A}) \) – coefficient of variation of plane section area, \( N_4 \) – number of \( \gamma' \) phase precipitates per unit area of plane section, \( L_4 \) – specific length of \( \gamma' \) phase precipitates boundaries, \( S_4 \) – specific surface of \( \gamma' \) phase precipitates boundaries, \( \delta \) – absolute error of measurement of plane section area of \( \gamma' \) phase precipitates.

**Statistical Analysis of \( A_4 \)**

The outcomes were measured at 8 different treatments, each with 2 replications. The analysis of effect revealed that only the HEIGHT factor affects significantly the outcome \( A_4 \) (see Table 2), which is indicated by \( p < 0.05 \). All other factors have an insignificant impact on the outcome \( A_4 \).

**TABLE 2**

<table>
<thead>
<tr>
<th>Term</th>
<th>Effect</th>
<th>SE</th>
<th>t</th>
<th>p</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constant</td>
<td>52.744</td>
<td>0.608</td>
<td>86.7</td>
<td>0.000</td>
</tr>
<tr>
<td>(1) Tech</td>
<td>-0.066</td>
<td>1.217</td>
<td>-0.054</td>
<td>0.958</td>
</tr>
<tr>
<td>(2) Height</td>
<td>-4.911</td>
<td>1.217</td>
<td>-4.04</td>
<td>0.004</td>
</tr>
<tr>
<td>(3) Trace</td>
<td>0.889</td>
<td>1.217</td>
<td>0.730</td>
<td>0.486</td>
</tr>
<tr>
<td>( 1 \times 2 )</td>
<td>0.739</td>
<td>1.217</td>
<td>0.607</td>
<td>0.561</td>
</tr>
<tr>
<td>( 1 \times 3 )</td>
<td>1.524</td>
<td>1.217</td>
<td>1.252</td>
<td>0.246</td>
</tr>
<tr>
<td>( 2 \times 3 )</td>
<td>-0.216</td>
<td>1.217</td>
<td>-0.178</td>
<td>0.863</td>
</tr>
</tbody>
</table>

The same results, however more spectacular, are presented in the Pareto plot of standardized effects (Fig. 7). The vertical line drawn at \( p = 0.05 \) marks a distinction between significant and insignificant effects.

In such a case, the fixed-effects model is reduced to only one-factor model:

\[
A_4 = 52.74 - 2.46 \cdot HEIGHT
\]

where \( HEIGHT \) is coded as (–1) for label 1 and (+1) for label 2. The determination factor yielded \( R^2 = 0.70 \). The residuals passed the test of normality at \( p = 0.995 \) (Shapiro-Wilk test).

The relationship between HEIGHT and outcome \( AA \) is presented in the marginal means plot (Fig. 8).

**Statistical analysis of \( \text{AREA} \)
(Plane section area)**

The outcomes were measured at 8 different treatments with different replications at each treatment. The analysis was conducted for the natural logarithm of the raw outcome AREA, because the data are relatively small and the regression model may return non-physical negative values. The substituted outcome was labeled LN(AREA).
The analysis of variance revealed that all but the three-way interaction affect LN(AREA) significantly (see Table 3), however interaction term HEIGHTxTRACE has a rather low impact (see Pareto plot Fig. 9). Significant terms are indicated by \( p < 0.05 \).

<table>
<thead>
<tr>
<th>Term</th>
<th>SS</th>
<th>df</th>
<th>MS</th>
<th>F</th>
<th>p</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constant</td>
<td>67424.22</td>
<td>1</td>
<td>67424.22</td>
<td>77696.52</td>
<td>0.000</td>
</tr>
<tr>
<td>(1)Tech</td>
<td>61.30</td>
<td>1</td>
<td>61.30</td>
<td>70.64</td>
<td>0.000</td>
</tr>
<tr>
<td>(2)Height</td>
<td>29.46</td>
<td>1</td>
<td>29.46</td>
<td>33.95</td>
<td>0.000</td>
</tr>
<tr>
<td>(3)Trace</td>
<td>157.43</td>
<td>1</td>
<td>157.43</td>
<td>181.42</td>
<td>0.000</td>
</tr>
<tr>
<td>1 × 2</td>
<td>12.57</td>
<td>1</td>
<td>12.57</td>
<td>14.48</td>
<td>0.000</td>
</tr>
<tr>
<td>1 × 3</td>
<td>11.02</td>
<td>1</td>
<td>11.02</td>
<td>12.70</td>
<td>0.000</td>
</tr>
<tr>
<td>2 × 3</td>
<td>4.19</td>
<td>1</td>
<td>4.19</td>
<td>4.82</td>
<td>0.028</td>
</tr>
<tr>
<td>1 × 2 × 3</td>
<td>0.03</td>
<td>1</td>
<td>0.03</td>
<td>0.03</td>
<td>0.861</td>
</tr>
<tr>
<td>Error</td>
<td>10587.03</td>
<td>12200</td>
<td>0.87</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

The same results may be presented in Pareto plot of standardized effects (Fig. 9).

The determination factor yielded \( R^2 = 0.70 \).

In such a case, the fixed-effects model includes constant, main (linear) effects and all two-way interactions:

\[
\begin{align*}
\text{AREA} = \exp & (-2.394 + 0.072 \cdot \text{TECH} + \\
& + 0.050 \cdot \text{HEIGHT} + 0.116 \cdot \text{TRACE} + \\
& - 0.031 \cdot \text{TECH} \times \text{TRACE} + \\
& + 0.019 \cdot \text{HEIGHT} \times \text{TRACE})
\end{align*}
\] (2)

where coding is as following:

<table>
<thead>
<tr>
<th>Factor</th>
<th>-1</th>
<th>+1</th>
</tr>
</thead>
<tbody>
<tr>
<td>TECH</td>
<td>the traditional core</td>
<td>the core covered with 5% modifier</td>
</tr>
<tr>
<td>HEIGHT</td>
<td>1</td>
<td>2</td>
</tr>
<tr>
<td>TRACE</td>
<td>M</td>
<td>B</td>
</tr>
</tbody>
</table>

The results of this investigation suggest that \( \gamma' \) phase precipitates in dendrite cores are characterized by:

- greater mean plane section area in the cross-sections with numbers 2 than in the cross-sections with numbers 1;
- greater volume fraction in the cross-sections with numbers 1 than in the cross-sections with numbers 2.

5. Conclusions

The presented complex procedure of a quantitative evaluation of the \( \gamma' \) phase precipitates of IN 713C superalloy containing a selection of the proper sample preparation, the image acquisition and the image analysis provides obtaining repeatable results.

In general, the impact of those factors on the LN(AREA) may be presented in Fig. 10, where smaller LN(AREA) relates to smaller AREA.
The type of a technology TECH does not affect the relative volume fraction of the $\gamma'$ phase precipitates. This outcome depends only on the HEIGHT factor defining the geometrical location of samples (cross-sections).

The type of a technology TECH strongly affects the plane section area of the $\gamma'$ phase precipitates (AREA), resulting in the larger area of these precipitates, however the impact depends on location defined by factors HEIGHT and TRACE, both defining the geometrical location of samples. The impact is the greatest for the location (HEIGHT=2; TRACE=M), lower and almost mutually equal for locations (HEIGHT=1; TRACE=M) and (HEIGHT=2, TRACE=B), and the lowest and non-significant for location (HEIGHT=1, TRACE=B). In the latter case, the mean area of objects is practically the same for both technologies.

It seems that one should use more sophisticated, but also more computationally expensive statistical non-parametric methods [14-16] in further investigation to reveal relationships between factors deeper than it is possible in a classic statistical analysis [12], however the computational cost of such enhancement is very high [17-18]. If the mesh of samples nodes in the space of factors is sparse, it would rather be explored by a factorial approach [19-21], while if the mesh is dense, the response surface methodology (RSM), particularly with the local approximation, seems to be more appropriate [22-23]. It may include specific non-parametric methods for the analysis of multi dimensional sparse data [24-25], even with a multiphysics approach [26-29], the fuzzy statistics [30-32] for uncertain data or the selection of dominant factors, derived from a production engineering [33].

![Image](Fig. 10. Impact of three input factors on the outcome LN(AREA))

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### REFERENCES


