# EQUILIBRIUM MODELING OF MONO AND BINARY SORPTION OF CU(II) AND ZN(II) ONTO CHITOSAN GEL BEADS

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The objective of the work are in-depth experimental studies of Cu(II) and Zn(II) ion removal on chitosan gel beads from both one- and two-component water solutions at the temperature of 303 K. The optimal process conditions such as: pH value, dose of sorbent and contact time were determined. Based on the optimal process conditions, equilibrium and kinetic studies were carried out. The maximum sorption capacities equaled: 191.25 mg/g and 142.88 mg/g for Cu(II) and Zn(II) ions respectively, when the sorbent dose was 10 g/L and the pH of a solution was 5.0 for both heavy metal ions. One-component sorption equilibrium data were successfully presented for six of the most useful three-parameter equilibrium models: Langmuir-Freundlich, Redlich-Peterson, Sips, Koble-Corrigan, Hill and Toth. Extended forms of Langmuir-Freundlich, Koble-Corrigan and Sips models were also well fitted to the two-component equilibrium data obtained for different ratios of concentrations of Cu(II) and Zn(II) ions (1:1, 1:2, 2:1). Experimental sorption data were described by two kinetic models of the pseudo-first and pseudo-second order. Furthermore, an attempt to explain the mechanisms of the divalent metal ion sorption process on chitosan gel beads was undertaken.

**Keywords:** chitosan, heavy metals, equilibrium modeling, binary solutions

## 1. INTRODUCTION

In the last decade, the presence of heavy metal ions in the environment has attracted attention of researches. The amount of heavy metal release into the environment is increasing as a result of development of industrial processes and technological expansion. The potential sources of heavy metal ions are industrial wastewaters which include: fertilizers, pigments, metal finishing etc. (Arh-Hwang et al., 2008; Tomczak, 2013). Waste streams containing Cu(II) originated from a variety of industries among others: meishing and copper electroplating, which cause a significant threat to aquatic life and make natural water unsuitable for public use (Alimohamadi et al., 2005; Hasan et al., 2008).

Zn(II) can be found in wastewater derived from various electroplating pollutants e.g.: acid mine drainage (AMD), electroplating and from municipal wastewater. Zn(II) is not biodegradable and can accumulate throughout the food chain, becoming a serious danger (Norton et al., 2004). Therefore Cu(II) and Zn(II) ions are among the most common heavy metals in industries wastewaters. The accumulation of Cu(II) ions in human body causes brain, skin and pancreas damage and heart diseases. Zn(II) ions are on the list of priority pollutants giving rise to serious poisoning cases.

The heavy metals, which are detrimental to one's health, can be removed from wastewater using various conventional methods such as: precipitation, reverse osmosis, chemical reduction, ion exchange

and physical sorption (Veli and Alyuz, 2007). However, the above processes proceed slowly and their effectiveness depends on many factors such as: the pH of a solution, the type of a heavy metal ions (oxidation state, type of complexes) and the concentration or the presence of other substances dissolved in water.

The biosorption process is an alternative to traditional methods of heavy metal removal from aqueous solutions. It is a biological purification method of wastewaters, based on the binding of metal ions on the biosorbent surface.

Chitosan is a low cost natural material, used for biosorption of heavy metal ions (Alimohamadi et al., 2005; Chen et al., 2008; Hasan et al., 2008; Norton et al., 2004; Sevil and Alyuz, 2007). Chitosan is a derivative of chitin, which can be extracted from fungi, and in large quantities, from the exoskeleton of crustaceans such as crabs, shrimps, krill and crawfish. In comparison with chitin, chitosan is more efficient in terms of sorption capacity. It is due to the presence of a large number of free amino groups on chitosan chain which are responsible for the high sorption capacity (Sankararamakrishnan et al., 2007). However, unlike chitin, chitosan is soluble in dilute organic acids, such as acetic or formic acids.

The most interesting fact, compared to other sorbents, is that chitosan can be processed into: flakes (Jha et al., 1987), beads (Baran et al., 2006) and membranes (Osifo et al., 2008). Chitosan can be physically and chemically modified to improve the sorption capacity and the chemical stability of chitosan in acid media (Kyzas and Bikiaris, 2015). Chitosan without modification has already high chemical stability in acid media. It is resistant to biochemical and microbiological degradation and most of all has high affinity for sorption of heavy metal ions.

Most of the studies dedicated to metal ion biosorption on various modified chitosan concern one component metal ion water solutions, although the real aquatic solutions generally consist of toxic heavy metal mixtures (Wan Ngah and Fatinathan, 2008).

Therefore the main objective of this study was to investigate the sorption process of copper (Cu(II)) and zinc (Zn(II)) ions from one- and two-component water solutions on unmodified chitosan gel beads.

#### 2. SORPTION MECHANISMS

Chitosan is a strongly complexing polymer in relation to heavy metal ions. Amino groups of chitosan chains in which nitrogen is the donor of electron pairs are responsible for the formation of such complexes (Jin and Bai, 2002; Onsosyen and Skaugrud, 1990; Rinaudo, 2006). Both nitrogen and oxygen atoms have lone pairs of electrons which can bind a proton of metal ion to form a complex (Onsoyen and Skaugrud, 1990). However, nitrogen atoms have stronger tendency to donate the lone pair of electrons with heavy metal ions to form a complex than the oxygen atom. Based on the above consideration, the process can proceed according to the following reaction (Jin and Bai, 2002):

$$R-NH_2 + H^+ \leftrightarrow R-NH_3^+ \tag{1}$$

This reaction indicates the protonation and deprotonation processes of amino groups in chitosan. The binding mechanism of the group with heavy metal ions is very specific and can depend on other factors, such as: pH value or type of metal ion. For example, at a lower pH of a solution more amino groups are protonated. Whereas at higher pH values, OH ions can be adsorbed to the surface of chitosan gel beads through a hydrogen bond (Jin and Bai, 2002; Rinaudo, 2006):

$$R-NH_2+OH^- \rightarrow R-NH_2 \bullet \bullet \bullet OH^-$$
 (2)

When heavy metal ions were added into the solution, the reaction proceded due to sharing of the lone pair of the electrons from the nitrogen atom with heavy metal ion, in the similar manner as reaction (Sankararamakrishnan et al., 2007):

$$R-NH_2 + M^{2+} \leftrightarrow R-NH_2M^{2+}$$
 (3)

However, the electrical attraction force between lone pair electrons from the nitrogen atom and the bivalent heavy metal ion can be stronger than that between the lone pair of electrons from the nitrogen atom and the monovalent proton (H<sup>+</sup>) (Jin and Bai, 2002; Onsoyen and Skaugrud, 1990; Rinaudo, 2006; Wang et al., 2004). From these differences in the force of the binding we can write another reaction described as follows:

$$R-NH_3^+ + M^{2+} \leftrightarrow R-NH_2M^{2+} + H^+$$
 (4)

In this reaction a competitive adsorption of  $M^{2+}$  over  $H^{+}$  to the nitrogen atom occurs, which can be considered as ion exchange mechanism (Jin and Bai, 2002; Onsosyen and Skaugrud, 1990). In comparison to reaction (3), reaction (4) can run slowly, due to smaller force attraction between the N in R-NH<sub>3</sub> and  $M^{2+}$  (Oyrton et al., 1999).

For the complex of R-NH<sub>2</sub>M<sup>2+</sup> it is greater binding force of M<sup>2+</sup> with the OH<sup>-</sup> group from water:

$$R-NH_2 M^{2+} + H_2O \leftrightarrow MOH^+ + R-NH_3^+$$
 (5)

This reaction together with reactions (2) and (4) make heavy metal ions be present in the complex of  $R-NH_2$   $M^{2+}$  rather than be distributed in the solution. Heavy metal sorption on chitosan gel beads can also be controlled by the transport of heavy metal ions from the solution bulk to the chitosan bead surface. The transport of heavy metal cation  $M^{2+}$  to the surface sites  $R-NH_3$  could be inhibited at very low pH of solution.

## 3. EXPERIMENTAL METHODS

#### 3.1. Materials

The chitosan flakes used in experiments were deacetylated approximately 85% and their dynamic viscosity (20 °C) was 3200 mPa·s. The chitosan was purchased from Biolog Biotechnologie und Logistic GmbH. Copper(II) sulfate (CuSO<sub>4</sub>) and zinc sulfate heptahydrate (ZnSO<sub>4</sub>·7H<sub>2</sub>O) used in the sorption experiments were purchased from Chempur and were of analytical grade.

# 3.1.1. Preparation of chitosan gel beads

Preparation of chitosan gel beads involves dissolving 17.5 g of chitosan flakes in 1L of 2% aqueous solution of acetic acid and leaving the solution for 24 h. Then the dissolved chitosan is subjected to filtration in order to remove any kind of contamination. The formation of drops involves the use of the pressure method, which consists of compressed air being brought to a container with a solution of chitosan. The chitosan solution was pressed through a capillary with a diameter of 2 mm finished with the blade to facilitate the formation of droplets. The diameter of chitosan gel beads was about 2.5 mm.

Discharged drops fell freely into the cylinder with a solution of 10% sodium hydroxide. The process was conducted by applying continuous mixing.

In the final step beads were washed with distilled water to remove any residues of sodium hydroxide. Before the sorption process chitosan gel beads were kept in distilled water at least seven days.

## 3.2. Sorption studies

# 3.2.1. pH effects

The effect of the pH of solutions on Cu(II) and Zn(II) sorption were examined by adding 10 g of wet chitosan beads (dry mass was related to wet one and was at a constant ratio in experiments) into 200 mL solutions containing Cu(II) and/or Zn(II) to 250 mL dark flasks. In one-component systems the ion initial concentration was constant and equaled 60 mg/L. In two-component solutions the Cu(II)-Zn(II) mixture of concentration ratio 1:1 was used in which each ion initial concentration was also constant and equaled 64 mg/L. These solutions were adjusted to pH 4.0, 5.0, 6.0 and 6.5 with 0.1 M hydrochloric acid or 0.1 M sodium hydroxide solution. Concentrations of solutions were measured with Inductively Coupled Plasma Spectrometer ICP-AES (Jobin Yvon, France). The sorption capacity was calculated using the relation:

$$q_e = \frac{C_0 - C_e}{m}V\tag{6}$$

## 3.2.2. Effect of sorbent dose

The dependence of metal ion sorption on the dose of chitosan gel beads was examined using various amounts of sorbent, ranging from 5 to 15 g wet chitosan beads into 200 mL solutions containing Cu(II) or Zn(II) in the concentration of 60 mg/L. Thus, the sorbent dose ranged from 25 to 75 g/L. Concentrations were also measured with Inductively Coupled Plasma Spectrometer ICP-AES.

## 3.2.3. Effect of contact time

Experiments of contact time effect were carried out by placing 10 g of wet chitosan beads into 200 mL solution containing Cu(II) or Zn(II) ions, with a sorbent dose of 50 g/L. Samples were stirred in an incubator shaker at a constant value of pH at 30 °C. Samples were agitated at 175 rpm for various periods of time. Then 30 mL of these solutions at some intervals of time were filtered and their concentrations were measured with ICP-AES. The sorption capacities were calculated from Eq. (6).

## 3.3. Sorption isotherms

Equilibrium batch sorption studies were carried out by placing 10 g of wet chitosan beads into 200 mL solutions containing Cu(II) and/or Zn(II) ions at various initial concentrations, with a sorbent dose of 50 g/L. The initial concentration of Cu(II) and Zn(II) ions in the one-component solutions ranged from 20 mg/L to 1200 mg/L. The initial concentration of Cu(II) and Zn(II) ions in two-component solutions ranged from 20 mg/L to 800 mg/L. The sorption equilibrium in two-component systems was studied in solutions containing Cu(II) and Zn(II) at different ratios of concentration 1:1, 1:2, 2:1. Then flasks were placed in an incubator shaker at 30 °C and were agitated at 175 rpm for various periods of time. The concentration of Cu(II) and Zn(II) ions in the solution was analyzed with ICP-AES.

#### 4. RESULTS AND DISCUSSION

# 4.1. FTIR study of the chitosan gel beads

Our studies of Fourier transform infrared spectroscopy (FTIR) of chitosan gel beads were performed to determine the molecular structure of intermolecular interactions between the components in chitosan

gel beads. FTIR absorption spectra show the absorbance dependence on the wave number. The results of FTIR spectra are shown in Fig. 1.

The major peaks of the chitosan gel beads are located around 3620 cm<sup>-1</sup> for –OH stretching vibration polysaccharide chain and 1651 cm<sup>-1</sup> for -NH<sub>2</sub> stretching vibration. Another peak at 2920-2860 cm<sup>-1</sup> can be attributed to –CH stretching vibrations. The carbonyl bond (C=O) derived from chitin can be observed in the spectrum of 1651 cm<sup>-1</sup>. The polysaccharide stretching vibration (C=H) is located around 1100 cm<sup>-1</sup>. The hydrogen bonds between the polysaccharide chains are broken at the expense of interaction with metal cations. Thus chitosan material becomes more amorphous. The peak at 1020 cm<sup>-1</sup> can be attributed to stretching vibration of the bond C-O in polysaccharide chains (Wu et al., 2008).

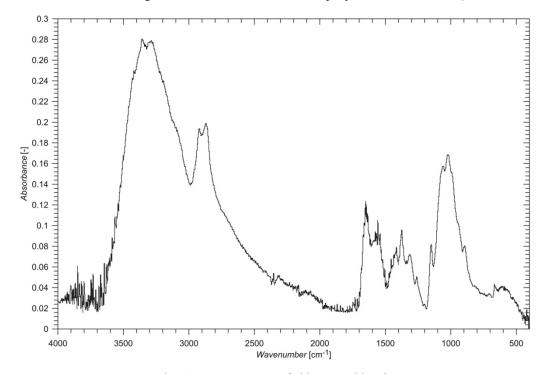


Fig. 1. FTIR spectrum of chitosan gel beads

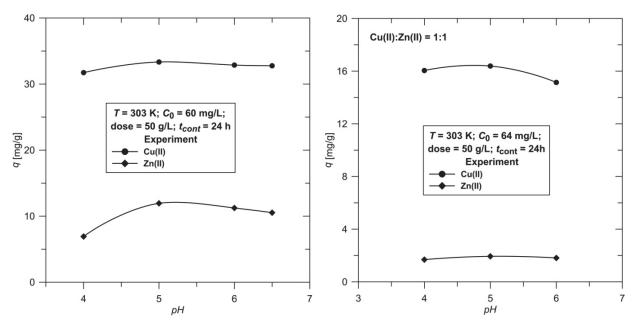


Fig. 2. pH effect on the sorption capacity of Cu(II) or Zn(II) ions on chitosan gel beads from one-component aqueous solutions

Fig. 3. pH effect on the sorption capacity of Cu(II) and Zn(II) ions on chitosan gel beads from two-component aqueous solution

# 4.2. Sorption effects

# 4.2.1. pH effects

The pH of a solution affects the adsorption capacity of chitosan. The effect of the pH of a solution on the sorption of Cu(II) and Zn(II) ions on chitosan gel beads was investigated in the range of pH from 4.0 to 6.5 and from 4.0 to 6.0 for one- and two-component systems, respectively. Higher values of solution pH were not tested due to the fact that in pH higher than 7 precipitation of Cu(II) or Zn(II) may occur. Results are shown in Figs 2 and 3. It can be seen from these figures that there is a slight increase in sorption capacity with an increase in solution pH. For both one- and two-component solutions it is evident that there are small differences in the sorption capacity for pH ranging between 5.0 and 6.0.

The maximum sorption capacity of Cu(II) and Zn(II) ions occurs at pH 5 for both metal ions. This is because in acidic solutions, more protons will be available to protonate amine groups to form groups – NH<sub>3</sub>, reducing the number of binding sites for the adsorption of Cu(II) and/or Zn(II). Whereas, at higher solution pH adsorption increases due to the decreased inhibitory effect of H<sup>+</sup> (Wan Ngah et al., 2005). Therefore heavy metal ions were better sorbed by chitosan at higher solution pH.

The optimum pH values were determined for Cu(II) and Zn(II) as pH 5.0 for one- and two- component solutions. The optimum pH values were used in further one-component experimental studies, such as the dose of chitosan gel beads or the contact time.

#### 4.2.2. Effect of sorbent dose

The dependence of metal ion sorption on the dose of wet chitosan gel beads was studied using various amounts of sorbent in the range of 25-75 g/L. Results in Fig. 4 show that the sorption capacities of metal ions in sorbent sample slightly increase with the increase of the sorbent dose. The sorption capacity of Cu(II) was considerably greater than that of Zn(II) in the dose range of 25-75 g/L.

#### 4.2.3. Effect of contact time

The effect of contact time on the sorption of Cu(II) and Zn(II) ions on chitosan gel beads was investigated and experimental results are presented in Figs 5 and 6. The effect of contact time is an important parameter because it reflects sorption kinetics. The concentration of metal ions in the sorbent increases rapidly at the initial sorption stage, and then remains constant. Sorption equilibrium was reached within about 1000 min for Cu(II) and 240 min for Zn(II).

The maximum value of metal ion concentration in relationship of  $q_t$  versus time t (contact time) at a constant ion concentration  $C_0$  is a separate point in sorption isotherm. Simultaneously, the relation of contact time is used in modeling of process kinetics (relationship of  $q_t$  versus t at the given  $q_e$ ). In order to investigate the sorption mechanism, rate constants of sorption kinetics have to be determined. The pseudo-first order kinetic model can be presented in a linear form (Repo et al., 2010):

$$\log(q_e - q_t) = \log q_e - \frac{k_1}{2.303}t\tag{7}$$

The pseudo-second order kinetic model can be presented in another linear form (Repo et al., 2010):

$$\frac{t}{q_t} = \frac{1}{k_2 q_e^2} + \frac{1}{q_e} t \tag{8}$$

Constants of pseudo-first and pseudo-second order kinetic models were determined by least squares method using the linear regression.

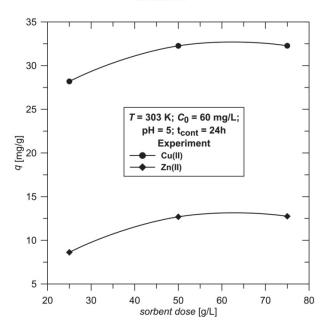


Fig. 4. Dose effect of chitosan gel beads on sorption capacity of Cu(II) ions and Zn(II) from one-component solutions

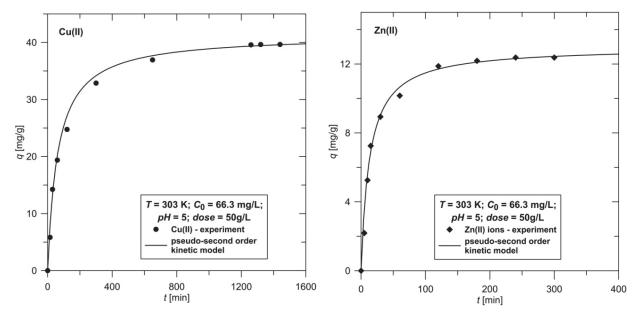


Fig. 5. Effect of contact time of chitosan gel beads in aqueous solution of Cu(II) ions on sorption capacity

Fig. 6. Effect of contact time of chitosan gel beads in aqueous solution of Zn(II) ions on sorption capacity

The average relative errors  $\delta$  [%], which are the measure of fit accuracy of rate constants to experimental data, were calculated from the following equation:

$$\delta = \frac{1}{N} \sum_{i=1}^{N} \left| \frac{q_{\exp_i} - q_{calc_i}}{q_{\exp_i}} \right| \tag{9}$$

The obtained values of pseudo-first order  $(k_1)$  and pseudo-second order  $(k_2)$  rate constants, the average relative errors  $(\delta)$  and determination coefficient  $(R^2)$  are shown in Table 1. It is evident that the pseudo-first order kinetic model gave a very poor approximation of the experimental data.

The correlated results of the pseudo-second order kinetic model for Cu(II) and Zn(II) ions, according to Eq. (8), are presented in Figs. 5 and 6, respectively.



Table 1. Approximated pseudo-first order and pseudo-second order kinetic rate constants for Cu(II) and Zn(II) ions on chitosan gel beads. *T*= 303 K, pH= 5, dose = 50 g/L

Heavy metal			Cu							
Pseudo-first order model					Pseudo-second order model					
$q_{ m exp}$ [mg/g]	զ <sub>cc</sub> [mջ		k <sub>1</sub> [min <sup>-1</sup> ]	δ [%]	R <sup>2</sup> [-]	$q_{ m exp}$ [mg/g]	$q_{calc} \ [ ext{mg/g}]$	$k_2$ [g/(mg·min)]	δ [%]	R <sup>2</sup> [-]
32.73	39.62		0.00668	17.38	0.608	39.62	41.49	0.000382	4.74	0.990
Heavy m	Heavy metal			Zn						
Pseudo-first order model				Pseudo-second order model						
$q_{ m exp}$ [mg/g]	զ <sub>cc</sub> [mg		$k_1$ [min <sup>-1</sup> ]	δ [%]	R <sup>2</sup> [-]	$q_{ m exp}$ [mg/g]	$q_{calc} \ [ ext{mg/g}]$	$k_2$ [g/(mg·min)]	δ [%]	R <sup>2</sup> [-]
12.31	3.4	40	0.0175	72.35	0.375	12.31	12.99	0.00588	5.48	0.990

For the second-order kinetic model the average relative error ( $\delta$ ) was 4.74% for Cu(II) ions and 5.48% for Zn(II) ions. Therefore the pseudo-second order kinetic model is better for describing the sorption kinetics of the analyzed heavy metals. Our data were also consistent with other literature data (Corrigan and Koble, 1952; Ho and McKay, 1999; Kousalya et al., 2010; Repo et al., 2010; Runping et al., 2006). Furthermore, it is known that when the pseudo-second order kinetic model shows the best fitting to the experimental data, the sorption mechanism involves chemisorption (Wang et al., 2012).

## 4.3. Sorption isotherm determination for one-component systems

The analysis of sorption process equilibrium requires determination of the isotherm. Sorption isotherm is the most significant factor for analyzing the nature of adsorbate-adsorbent interaction. The sorption equilibrium studies of Cu(II) and Zn(II) ions on chitosan gel beads were described by six of the most common three-parameter equilibrium models: Langmuir-Freundlich, Redlich- Peterson, Sips and Koble-Corrigan, Hill and Toth.

Langmuir-Freundlich isotherm equation is a modification of the Langmuir and Freundlich equilibrium models providing a common isotherm equation called Langmuir-Freundlich (Chen, 2013; Wang et al., 2012; Hamdaoui and Naffrechoux, 2007; Kousalya et al., 2010; Onsosyen and Skaugrud 1990; Oyrton et al., 1999; Repo et al., 2010; Rinaudo, 2006; Wang et al., 2004):

$$q_e = \frac{q_{mLF} K_{LF} C_e^{n_{LF}}}{1 + K_{LF} C_e^{n_{LF}}} \tag{10}$$

The three-parameter Redlich-Peterson equilibrium model is another combination of Freundlich and Langmuir equilibrium models and is intended to describe the heterogeneity of the sorbent surface. The Redlich-Peterson isotherm equation is given by (Repo et al., 2010):

$$q_e = \frac{K_{RP}C_e}{1 + B_{RP}C_e^{n_{RP}}} \tag{11}$$

Koble-Corrigan equilibrium model is also a three-parameter empirical model which is also another combination of the Langmuir and Freundlich isotherm equations. Koble-Corrigan equilibrium model is given by (Han et al., 2005):

$$q_e = \frac{K_{KC} C_e^{n_{KC}}}{1 + B_{KC} C_e^{n_{KC}}} \tag{12}$$

Sips proposed one more equation similar in form to the Langmuir-Freundlich isotherm equation (Chen, 2013; Repo et al, 2010):

$$q_e = \frac{q_{mS} (K_S C_e)^{n_S}}{1 + (K_S C_e)^{n_S}}$$
 (13)

Hill isotherm equation describes the binding of different species on homogeneous sorbent surface. This model assumes that sorption is a phenomenon concerned with the binding abilities of ligands at one site on the macromolecule. It may influence different binding sites of the same macromolecule (Chen, 2013):

$$q_e = \frac{q_{mH} C_e^{n_H}}{K_H + C_e^{n_H}} \tag{14}$$

Toth proposed an equilibrium model which is expressed in the following form (Lodeiro et al., 2005):

$$q_e = \frac{q_{mT} K_T C_e}{(1 + (K_T C_e)^{n_T})^{1/n_T}}$$
 (15)

Table 2. Approximated parameters and average relative errors of various equilibrium models for Cu(II) and Zn(II) ions on the chitosan gel beads

Langmuir-Freundlich isotherm constants					Redlich-Peterson isotherm constants				
	$q_{mLF}$ [mg/g]	$K_{LF}$ [L/mg]	$n_{LF}$ [-]	δ [%]		$K_{RP}$ [L/g]	$B_{RP}$ [L/mg]	$n_{RP}$ [-]	δ [%]
Cu <sup>2+</sup>	283.63	0.1027	0.454	3.06	Cu <sup>2+</sup>	50.94	1.0387	0.792	8.38
$Zn^{2+}$	145.11	0.0001	1.973	5.61	$Zn^{2+}$	0.705	0.0006	1.276	50.03
Koble-Corrigan isotherm constants					Sips isotherm constants				
	$K_{KC}$ [L/g]	$B_{KC}$ [L/mg]	$n_{KC}$ [-]	δ [%]		$q_{mS}$ [mg/g]	$K_S$ [L/mg]	$n_S$ [-]	δ [%]
$Cu^{2+}$	29.12	0.1027	0.454	3.06	Cu <sup>2+</sup>	283.57	0.0067	0.455	3.06
$Zn^{2+}$	0.012	0.0001	1.973	12.36	$Zn^{2+}$	144.29	0.0084	2.030	6.36
Hill isotherm constants						Toth i	sotherm const	ants	
	$q_{mH}$ [mg/g]	$K_H$ [mg/L]	$n_H$ [-]	δ [%]		$q_{mT}$ [mg/g]	$K_T$ [L/mg]	$n_T$ [-]	δ [%]
$Cu^{2+}$	283.64	9.741	0.454	3.05	Cu <sup>2+</sup>	61.34	1.049	0.792	34.83
$Zn^{2+}$	144.29	16390.2	2.029	6.36	Zn <sup>2+</sup>	178.91	0.00216	1.577	25.03

The constants of the Langmuir-Freundlich (Eq. (10)), Redlich-Peterson (Eq. (11)) Koble-Corrigan (Eq. (12)), Sips (Eq. (13)), Hill (Eq. (14)) and Toth (Eq. (15)) equilibrium models were fitted to the experimental data of Cu(II) and Zn(II) ions and results are shown in Table 2. These fitted constants were determined using the quasi-Newton nonlinear estimation method with Statistica software.

The equilibrium models fitted to the one-component sorption experimental data of Cu(II) and Zn(II) ions on chitosan gel beads are shown in Figs. 7 and 8. The obtained maximum sorption capacities  $(q_m)$  equaled 191.25 mg/g for Cu(II) ions (Fig. 7) and 142.88 mg/g for Zn(II) ions (Fig. 8).

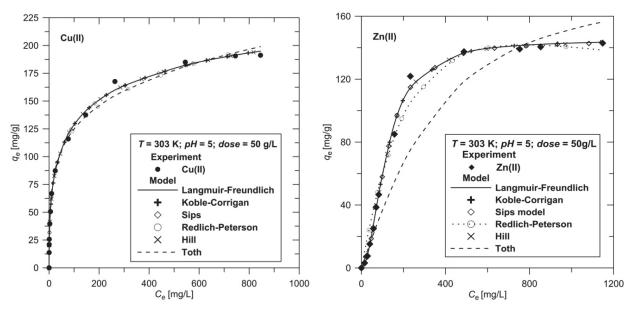


Fig. 7. Experimental and fitted sorption isotherms of Cu(II) ions on chitosan gel beads using various equilibrium models

Fig. 8. Experimental and fitted sorption isotherms of Zn(II) ions on chitosan gel beads using various equilibrium models

From analysis of Table 2 it can be concluded that the Langmuir-Freundlich, Hill and Sips equilibrium models approximate well the sorption behavior. These isotherm functions overlap in Figs. 7 and 8. Their average relative error ( $\delta$ ) for Cu(II) is about 3%. For Zn(II) the errors are similar and vary in the range from 5.61% to 6.36%. Also Koble-Corrigan equilibrium model quite well describes the experimental data. Its average relative error for Cu(II) has the same low value as the best models (  $\delta$ =3.06%). However, the error for Zn(II) ions is greater ( $\delta$  = 12.36%). Redlich-Peterson and Toth model gave the worst fitting results with high errors, especially for Zn(II) ions.

Based on the average relative errors ( $\delta$ ) for both metal ions, the equilibrium models fit accuracy to the experimental data of Cu(II) and Zn(II) ions is in the following order: Langmuir-Freundlich > Hill > Sips > Koble-Corrigan > Redlich-Peterson > Toth.

### 4.4. Sorption isotherm determination for two-component systems

In the last decade there were several examples of empirical isotherm models, which provide parameters derived from a one-component system. Unfortunately, some models fail when interactions between metals in the mixture occur. The maximum sorption capacity  $(q_m)$  and heterogeneity factor (n) depend on the concentrations of other components in the mixture. Therefore, the most desirable approach to two-component system modeling is an estimation of two-component isotherm on the basis of the association constant derived from one-component isotherms:  $K_{LF}$ ,  $K_{RP}$ ,  $K_{KC}$ ,  $K_{S}$ ,  $K_{H}$ ,  $K_{T}$  for Langmuir-Freundlich, Redlich-Peterson, Koble-Corrigan, Sips, Hill and Toth, respectively. In our study, the equilibrium data of two-component systems was modeled using the extended forms of the threeparameter isotherm equations such as: Langmuir-Freundlich, Koble-Corrigan, Sips, Redlich-Peterson, Hill and Toth. They are presented in Table 3.

These modeling calculations were carried out using Maple software (Maplesoft) by means of nonlinear programming based on the modified Newton method. Unknown parameters were estimated by minimizing the objective function e (Qi, 2003) for combined data of all concentration ratios:

$$e = \sum_{i} \sum_{j} (q_{\exp_{ij}} - q_{calc_{ij}})^{2}$$
 (16)

where i and j are the first and second component in the particular two-component mixture.

Table 3. Extended forms of the three-parameter isotherm equations for two metal ions

Two-component isotherm	Equation system	Literature
Langmuir- Freundlich	$q_{e1} = \frac{q_{m1LF} K_{1LF} C_{1e}^{m_1 LF}}{1 + K_{1LF} C_{1e}^{m_1 LF} + K_{2LF} C_{2e}^{n_2 LF}}$ $q_{e2} = \frac{q_{m2LF} K_{2LF} C_{2e}^{n_2 LF}}{1 + K_{1LF} C_{1e}^{n_1 LF} + K_{2LF} C_{2e}^{n_2 LF}}$	(Vieira et al., 2007)
Redlich-Peterson	$q_{e1} = \frac{K_{1RP}C_{1e}}{1 + B_{1RP}C_{1e}^{n_{1RP}} + B_{2RP}C_{2e}^{n_{2RP}}}$ $q_{e2} = \frac{K_{2RP}C_{2e}}{1 + B_{1RP}C_{1e}^{n_{1}RP} + B_{2RP}C_{2e}^{n_{2}RP}}$	(Sulaymon et al., 2011)
Koble-Corrigan	$q_{e1} = \frac{K_{1KC}C_{1e}^{n_1KC}}{1 + B_{1KC}C_{1e}^{n_1KC} + B_{2KC}C_{2e}^{n_2KC}}$ $q_{e2} = \frac{K_{2KC}C_{2e}^{n_2KC}}{1 + B_{1KC}C_{1e}^{n_1KC} + B_{2KC}C_{2e}^{n_2KC}}$	(Nastaj, 2013)
Sips	$q_{e1} = \frac{q_{m1S}(K_{1S}C_{1e})^{n_{1S}}}{1 + (K_{1S}C_{1e})^{n_{1S}} + (K_{2S}C_{2e})^{n_{2S}}}$ $q_{e2} = \frac{q_{m2S}(K_{2S}C_{2e})^{n_{2S}}}{1 + (K_{1S}C_{1e})^{n_{1S}} + (K_{2S}C_{2e})^{n_{2S}}}$	(Al-Asheh et al., 2000; Repo et al., 2010)
Hill	$q_{e1} = \frac{q_{m1H}C_{1e}^{m_1H}}{K_{1H} + C_{1e}^{m_1H} + K_{2H} + C_{2e}^{n_2H}}$ $q_{e2} = \frac{q_{m2H}C_{2e}^{n_2H}}{K_{1H} + C_{1e}^{m_1H} + K_{2H} + C_{2e}^{n_2H}}$	(Al-Asheh et al., 2003)
Toth	$q_{e1} = \frac{q_{m1T}K_{1T}C_{1e}^{n_1T}}{(1 + (K_{1T}C_{1e})^{n_1T})^{1/n_1T} + (1 + (K_{2T}C_{2e})^{n_2T})^{1/n_2T}}$ $q_{e2} = \frac{q_{m2T}K_{2T}C_{2e}^{n_2T}}{(1 + (K_{1T}C_{1e})^{n_1T})^{1/n_1T} + (1 + (K_{2T}C_{2e})^{n_2T})^{1/n_2T}}$	(Allen et al., 2004)

Two-component sorption studies were conducted in three initial concentration ratios (Cu(II)-Zn(II) 1:1, 1:2, 2:1) at a constant pH, constant sorbent dose and constant temperature. The initial concentrations were in the range of 22.224-1135.392 mg/L for Cu(II) ions and 20.416-1377.312 mg/L for Zn(II) ions. Results are presented in Table 4 and Figs. 9 through 11.

Very high values of the average relative errors  $\delta$  % were obtained for extended models of Redlich-Peterson and Toth. Thus, results of these two-component models are unsuitable for description of Cu(II) and Zn(II) ion sorption and therefore are not presented here. Hill model was also omitted due to similarity of obtained results to those for Sips isotherm.

For the one-component systems it was evident that sorption capacity of Cu(II) was insignificantly higher than that for Zn(II) ions (Figs 7 and 8). For two-component sorption studies, the maximum sorption capacity of Cu(II) ions was seven to twelve times higher than that of Zn(II) ions, for all the studied systems (Figs. 9 through 11).

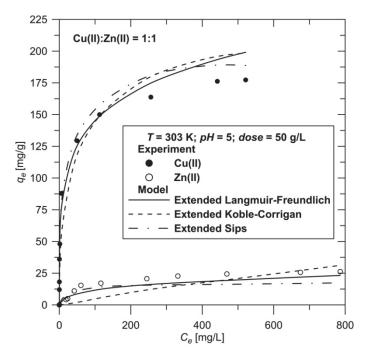
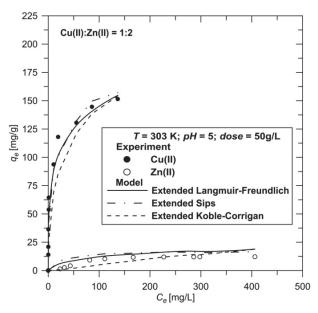


Fig. 9. Relationship of adsorption capacities of Cu(II) and Zn(II) on chitosan gel beads versus metal ion concentration in two-component equilibrium-initial concentration ratio 1:1. Experimental and various isotherm modeling data

Table 4. Approximated parameters and average relative errors of various extended equilibrium models for sorption of Cu(II) and Zn(II) ion mixture on chitosan gel beads

Extended Langmuir-Freundlich model						
$q_{m1LF}$ [mg/g] $K_{1LF}$ [L/mg]		<i>n</i> <sub>1<i>LF</i></sub> [-]	$q_{m2LF}$ [mg/g]	$K_{2LF}$ [L/mg]	n <sub>2LF</sub> [-]	
528.98	0.103	0.284	16957.99	0.000080	0.497	
$\delta_{1,1:1}$ (%)	δ <sub>1,2:1</sub> (%)	δ <sub>1.1:2</sub> (%)	$\delta_{2,1:1}$ (%)	δ <sub>2,2:1</sub> (%)	δ <sub>2,1:2</sub> (%)	
20.13	18.33	15.65	22.09	12.56	75.75	
	Extended Koble-Corrigan model					
$B_{1KC}$ [L/mg] $K_{1KC}$ [L/g]		<i>n</i> <sub>1<i>KC</i></sub> [-]	$B_{2KC}$ [L/mg]	$K_{2KC}$ [L/g]	$n_{2KC}$ [-]	
0.074	29.12	0.469	0.00005	0.012	1.337	
$\delta_{1,1:1}$ (%)	$\delta_{1,2:1}$ (%)	$\delta_{1,1:2}$ (%)	$\delta_{2,1:1}$ (%)	$\delta_{2,2:1}$ (%)	$\delta_{2,1:2}$ (%)	
22.12	12.21	29.46	47.89	37.64	34.54	
Extended Sips model						
$q_{m1S}$ [mg/g]	$K_{1S}$ [L/mg]	$n_{1S}$ [-]	$q_{m2S}$ [mg/g]	$K_{2S}$ [L/mg]	$n_{2S}$ [-]	
656.0292	0.00667	0.394	32.38	0.00838	0.591	
$\delta_{1,1:1}$ (%)	$\delta_{1,2:1}$ (%)	$\delta_{1,1:2}$ (%)	$\delta_{2,1:1}$ (%)	$\delta_{2,2:1}$ (%)	$\delta_{2,1:2}$ (%)	
19.10	21.82	14.65	32.59	11.70	107.39	



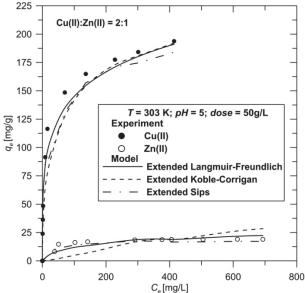


Fig. 10. Relationship of adsorption capacities of Cu(II) and Zn(II) on chitosan gel beads versus metal ion concentration in two-component equilibrium-initial concentration ratio 1:2. Experimental and various isotherm modeling data

Fig. 11. Relationship of adsorption capacities of Cu(II) and Zn(II) on chitosan gel beads versus metal ion concentration in two-component equilibrium-initial concentration ratio 2:1. Experimental and various isotherm modeling data

From analysis of Figs. 9 through 11 one can conclude that the extended Langmuir-Freundlich model describes generally fairly well the sorption behavior in the two-component systems, except Zn(II) in the presence of Cu(II) for the concentration ratio of 1:2 ( $\delta_2 = 75.75\%$ ). In other systems and concentration ratios, the error values vary from 12.56% to 22.09%.

The extended Sips model gave the best fitting to the experimental data for the concentration ratio of 1:1 (Fig. 9) for Cu(II) in the presence of Zn(II). The average relative error ( $\delta_1$ ) equals 19.10%, However, for Zn(II) ions in the presence of Cu(II) ions the average relative error ( $\delta_2$ ) is higher and equals 32.59%. Taking into account both concentration ratios, relative errors for the extended Langmuir-Freundlich model ( $\delta_1$  = 20.13%,  $\delta_2$  = 22.09%) are more uniformly distributed.

For the concentration ratio of 1:2, the most uniformly distributed average relative errors are obtained for Koble-Corrigan model ( $\delta_1$  = 29.46%,  $\delta_2$  = 34.54%). Langmuir-Freundlich and Sips models gave lower values of the average relative errors only for Cu(II) in the presence of Zn(II) ions ( $\delta_1$  = 15.65% and  $\delta_1$  = 14.65%, respectively) and definitely higher values for Zn(II) ions in the presence of Cu(II) ions ( $\delta_2$  = 75.75%,  $\delta_2$  = 107.39%, respectively).

Whereas, for the concentration ratio of 2:1 (Figure 11), for Cu(II) in the presence of Zn(II), the best fitting is provided by the extended Langmuir-Freundlich model. The average relative error ( $\delta_1$ ) for Cu(II) ions in the presence of Zn(II) ions equals 18.33% and for Zn(II) ions in the presence of Cu(II) ions ( $\delta_2$ ) equals 12.56%. A slightly worse, but fairly good approximation is exhibited by the Sips model ( $\delta_1$ = 21.82%,  $\delta_2$ = 11.70%).

## 5. CONCLUSIONS

In the study, sorptive removal of Cu(II) and Zn(II) ions from one- and two-component solutions on chitosan gel beads was investigated at 303 K. The sorption of metal ions was not strongly depended on the pH of a solution and the dose of sorbent. Maximum heavy metal removal capacities from water solutions were obtained at pH=5.0 for Cu(II) and Zn(II) ions both in the one- and two-component

systems. The optimum dose of sorbent was determined as 50 g/L for all studied heavy metals. Equilibrium contact times were reached: for Cu(II) within about 1000 min, whereas for Zn(II) ions within 240 min. It was proved that the pseudo-second order kinetic model is adequate to describe the sorption kinetics of the mentioned heavy metals onto chitosan gel beads, which is consistent with other reports.

An attempt was made to explain sorption mechanism of the investigated heavy metals on chitosan gel beads. Amino groups of chitosan chain in which nitrogen is donor of the electron pairs are mainly responsible for the formation of complexes with heavy metal cations (Jin and Bai, 2002). Additionally, this mechanism depends on other factors such as: the pH of a solution, deacylation process and chitosan form.

The maximum sorption capacities  $(q_m)$  in one-component solutions equaled 191.25 mg/g for Cu(II) ions and 142.88 mg/g for Zn(II) ions.

Six, most common three-parameter equilibrium models: Langmuir- Freundlich, Redlich-Peterson, Sips, Koble-Corrigan, Hill and Toth, were fitted to one-component experimental equilibrium sorption data. The accuracy of equilibrium model fittings for Cu(II) and Zn(II) ions were in the following order: Langmuir-Freundlich > Hill > Sips > Koble-Corrigan > Redlich-Peterson > Toth. Finally, two-component equilibrium data were described by the extended Langmuir-Freundlich, Koble-Corrigan and Sips models, which were based on the previous modeling results obtained for the one-component systems. The overall best fitting accuracy was obtained for the Langmuir-Freundlich model.

As a result of the study, one can draw a conclusion that chitosan gel beads can be successfully used for removal of heavy metals both from one-component and two-component solutions. It can be attributed to strong affinity of chitosan gel beads to heavy metals. Additionally, chitosan gel beads are relatively easily manufactured and are therefore abundant sorbents. For this reason they can be recommended for use in the removal of heavy metals from wastewater.

This study was funded by development and research project for young scientist 517-10-013-3579/17.

## **SYMBOLS**

$B_{KC}$	one-component Koble-Corrigan constant, L/mg
$B_{RP}$	one-component Redlich-Peterson constant, L/mg
$B_{IKC}$	Koble-Corrigan constant for Cu(II) in two-component mixture, L/mg
$B_{IRP}$	Redlich-Peterson constant for Cu(II) in two-component mixture, L/mg
$B_{2KC}$	Koble-Corrigan constant for Zn(II) in two-component mixture, L/mg
$B_{2RP}$	Redlich-Peterson constant for Zn(II) in two-component mixture, L/mg
$C_e$	equilibrium liquid phase concentration of metal ion, mg/L
$C_{\theta}$	initial concentration of metal ion, mg/L
$C_{le}$	equilibrium liquid phase concentration of Cu(II) ion in two-component mixture, mg/L
$C_{2e}$	equilibrium liquid phase concentration of Zn(II) ion in two-component mixture, mg/L
$k_{I}$	rate constant of pseudo-first order kinetic model, min <sup>-1</sup>
$k_2$	rate constant of pseudo-second order kinetic model, g/(mg min)
$K_H$	one-component Hill isotherm constant, mg/L
$K_{KC}$	one-component Koble-Corrigan isotherm constant, L/g
$K_{LF}$	one-component Langmuir-Freundlich isotherm constant, L/mg
$K_{RP}$	one-component Redlich-Peterson isotherm constant, L/g
$K_S$	one-component Sips isotherm constant, L/mg
$K_T$	one-component Toth model constant, L/mg

$K_{IH}$	Hill isotherm constant for Cu(II) in two-component mixture, mg/L
$K_{IKC}$	Koble-Corrigan isotherm constant for Cu(II) in two-component mixture, L/g
$K_{ILF}$	Langmuir-Freundlich isotherm constant for Cu(II) in two-component mixture, L/mg
$K_{IRP}$	Redlich-Peterson isotherm constant for Cu(II) in two-component mixture, L/g
$K_{IS}$	Sips isotherm constant for Cu(II) in two-component mixture, L/mg
$K_{IT}$	Toth model constant for Cu(II) in two-component mixture, L/mg
$K_{2H}$	Hill isotherm constant for Zn(II) in two-component mixture, mg/L
$K_{2KC}$	Koble-Corrigan isotherm constant for Zn(II) in two-component mixture, L/g
$K_{2LF}$	Langmuir-Freundlich isotherm constant for Zn(II) in two-component mixture, L/mg
$K_{2RP}$	Redlich-Peterson isotherm constant for Zn(II) in two-component mixture, L/g
$K_{2S}$	Sips isotherm constant for Zn(II) in two-component mixture, L/mg
$K_{2T}$	Toth model constant for Zn(II) in two-component mixture, L/mg
m	weight of the dry chitosan beads, g
N	number of data points
$n_H$	one-component sorbent heterogeneity constant of Hill isotherm
$n_{KC}$	one-component sorbent heterogeneity constant of Koble-Corrigan isotherm
$n_{LF}$	one-component sorbent heterogeneity constant of Langmuir-Freundlich isotherm
$n_{RP}$	one-component sorbent heterogeneity constant of the Redlich-Peterson isotherm
$n_S$	one-component sorbent heterogeneity constant of Sips isotherm
$n_T$	one-component sorbent heterogeneity constant of Toth isotherm
$n_{1H}$	sorbent heterogeneity constant of Hill isotherm for Cu(II) in two-component mixture
$n_{IKC}$	sorbent heterogeneity constant of Koble-Corrigan isotherm for Cu(II) in two-component
· · · · · ·	mixture
$n_{ILF}$	sorbent heterogeneity constant of Langmuir-Freundlich isotherm for Cu(II) in two-
	component mixture
$n_{IRP}$	sorbent heterogeneity constant of the Redlich-Peterson isotherm for Cu(II) in two-
	component mixture
$n_{IS}$	sorbent heterogeneity constant of Sips isotherm for Cu(II) in two-component mixture
$n_{IT}$	sorbent heterogeneity constant of Toth isotherm for Cu(II) in two-component mixture
$n_{2H}$	sorbent heterogeneity constant of Hill isotherm for Zn(II) in two-component mixture
$n_{2KC}$	sorbent heterogeneity constant of Koble-Corrigan isotherm for Zn(II) in two-component
	mixture
$n_{2LF}$	sorbent heterogeneity constant of Langmuir-Freundlich isotherm forZn(II) in two-component mixture
$n_{2RP}$	sorbent heterogeneity constant of the Redlich-Peterson isotherm for Zn(II) in two-
	component mixture
$n_{2S}$	sorbent heterogeneity constant of Sips isotherm for Zn(II) in two-component mixture
$n_{2T}$	sorbent heterogeneity constant of Toth isotherm for Zn(II) in two-component mixture
q	experimental sorption capacity on chitosan gel beads, mg/g
$q_e$	one-component equilibrium sorption capacity on chitosan gel beads, mg/g
$q_{el}$	Cu(II) ions equilibrium sorption capacity on chitosan gel beads in two-component
1	mixture, mg/g
$q_{e2}$	Zn(II) ions equilibrium sorption capacity on chitosan gel beads in two-component
<b>A</b> *	mixture, mg/g
$q_m$	component maximum adsorption capacity, mg/g
$q_{mH}$	one-component Hill maximum adsorption capacity, mg/g
$q_{mLF}$	one-component Langmuir-Freundlich maximum adsorption capacity, mg/g
$q_{mS}$	one-component Sips maximum adsorption capacity, mg/g
$q_{mT}$	one-component Toth maximum adsorption capacity, mg/g
$q_{m1H}$	Hill maximum adsorption capacity of Cu(II) in two-component mixture, mg/g
$q_{m1LF}$	Langmuir-Freundlich maximum adsorption capacity of Cu(II) in two-component
Amira.	mixture made

mixture, mg/g

$q_{m1S}$	Sips maximum adsorption capacity of Cu(II) in two-component mixture, mg/g
$q_{m1T}$	Toth maximum adsorption capacity of Cu(II) in two-component mixture, mg/g
$q_{m2H}$	Hill maximum adsorption capacity of Zn(II) in two-component mixture, mg/g
$q_{m2LF}$	Langmuir-Freundlich maximum adsorption capacity of Zn(II) in two-component
	mixture, mg/g
$q_{m2S}$	Sips maximum adsorption capacity of Zn (II) in two-component mixture, mg/g
$q_{m2T}$	Toth maximum adsorption capacity of Zn (II) in two-component mixture, mg/g

amounts of metal ions sorbed on chitosan gel beads at time t, mg/g

t time, min  $t_{cont}$  contact time, h

V volume of solution of metal ions, L

#### Subscripts

 $q_t$ 

exp experimental calc calculated

*i* first component in the particular two-component mixture *j* second component in the particular two-component mixture

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Received 29 January 2016 Received in revised form 24 August 2016 Accepted 30 August 2016