STATISTICAL PROCESS CONTROL OF COMMERCIAL FORCE-SENSING RESISTORS

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Abstract

The manufacturing and characterization of polymer nanocomposites is an active research trend nowadays. Nonetheless, statistical studies of polymer nanocomposites are not an easy task since they require several factors to consider, such as: large amount of samples manufactured from a standardized procedure and specialized equipment to address characterization tests in a repeatable fashion. In this manuscript, the experimental characterization of sensitivity, hysteresis error and drift error was carried out at multiple input voltages ($U_s$) for the following commercial brands of FSRs (force sensing resistors): Interlink FSR-402 and Peratech SP200-10 sensors. The quotient between the mean and the standard deviation was used to determine dispersion in the aforementioned metrics. It was found that a low mean value in an error metric is typically accompanied by a comparatively larger dispersion, and similarly, a large mean value for a given metric resulted in lower dispersion; this observation was held for both sensor brands under the entire range of input voltages. In regard to sensitivity, both sensors showed similar dispersion in sensitivity for the whole range of input voltages. Sensors’ characterization was carried out in a tailored test bench capable of handling up to 16 sensors simultaneously; this let us speed up the characterization process.

Keywords: force sensing resistors (FSR), pressure sensor, statistical process control, hysteresis error, drift error.

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1. Introduction

Polymer nanocomposites have gained great attention in recent years due to multiple front-end applications that have been developed. Besides the traditional applications of strain and stress sensing [1–4], polymer nanocomposites have also found acceptance in chemical and pollutant sensing, e.g. Fernandez et al. have successfully developed ammonia sensors through the combination of polypyrrole with other polymers [5]. Similarly, Lu et al. have developed composite materials capable of measuring chemical vapours of dimethylformamide, ammonia, and physical
variables such as temperature and strain [6]; this kind of multi-variable sensor was developed through the combination of graphite nanosheets with polyamide. Other studies reporting the usage of nanocomposites for vapour and gas sensing can be found in the review article from Shukla and Saxena [7]. The main benefits of polymer nanocomposites over other sensing solutions can be explained with the ease of manufacturing, low cost and high availability of polymers and fillers [8].

Despite multiple studies reporting polymer nanocomposites and their applications [8–11], only few studies have embraced a statistical approach to evaluate the performance of polymer nanocomposites. More specifically, statistical tools have been primarily employed to study the effect of a design parameter on sensor’s sensitivity, but they have not been extensively used to assess the statistical distribution of hysteresis, drift and other error metrics. To exemplify this, we can mention the studies from Saleh et al. [12], and Yuan and Lin [13]. Saleh et al. embraced T-Tests to study the effect of either using polylactic acid or polyurethane to assemble health monitoring sensors [12]. Likewise, Yuan and Lin used tools from Principal Component Analysis (PCA) to identify interactions of ammonia and chloroform with nanocomposites manufactured from multiple polymers and Carbon Nanotubes (CNTs) [13]. Similar approaches have been reported in the studies from Speller et al. [14], and Jaffal et al. [15].

Following the previous statement, a great effort has been also placed on the manufacturing of aerogels comprising carbon nanofibers and conductive polymers as means of strain sensing [16, 17]. Similarly, multiple authors have explored nanocomposites with multiple fillers to enhance sensor performance [18, 19], and more recently, self-healing properties have been incorporated to stress/strain sensors [20, 21]. On the other hand, only few studies have employed statistical tools to comparatively analyse the performance metrics of polymer nanocomposites aimed for stress/strain sensing; this is the case of the studies by Hall et al. [22], Komi et al. [23], Dabling et al. [24], and Hollinger and Wanderley [25]. Nonetheless, such studies have mostly embraced a reduced number of sensors in the assessment of the following performance metrics: hysteresis error, drift error, repeatability error and sensitivity degradation. Naturally, a reduced number of sensors cannot provide us with an adequate framework for statistical analysis, and for this reason, a different approach was taken up in this research.

We can only hypothesize possible reasons that keep researchers away from statistical studies in polymer nanocomposites. Considering that statistical studies require large sample counts, cost and manufacturing time are major factors to consider. However, according to the authors’ criteria, the most powerful reason is the inability of most research labs to manufacture and test large amounts of sensors following a standardized procedure. Depending on the methodology used, it is requires between 40 and 100 specimens to obtain statistically representative results; these quantities may not seem too large from a manufacturing standpoint, but during testing and characterization, these quantities are simply too large because most research labs are equipped with one-specimen measuring equipment. Moreover, some test protocols involve settling times of nearly one hour which dramatically increases the length of the characterization process.

Based on previous observations, this study comprised the statistical characterization of two commercial brands of Force Sensing Resistors (FSRs) manufactured from a blend of insulating polymer and carbon black. The sensors chosen for this study were: Interlink FSR402, manufactured by Interlink Electronics, Inc. (Westlake Village, CA, USA) and Peratech SP200-10, manufactured by Peratech Holdco Limited (Sedgefield, UK). The characterization involved sensitivity, hysteresis and drift tests. In order to overcome the requirements of a lengthy characterization, a tailored test bench has been designed and built which is capable of handling up to 16 sensors simultaneously. With the aim of obtaining statistically representative results, a total of 48
specimens from each brand were evaluated; this let us assess not only the average of a given performance metric, but also its dispersion.

The rest of this paper is organized as follows: the experimental setup and characterization procedure is presented in Section 2, followed by the experimental results and discussion in Section 3. Finally, conclusions are stated in Section 4.

2. Experimental setup and characterization procedure

The entire characterization procedure was done with a tailored test bench capable of handling up to 16 sensors simultaneously using a sandwich-like configuration, see Fig. 1. Forces were applied from a linear stepper motor model L5918L3008, manufactured by Nanotec Electronic GmbH & Co (Feldkirchen, Germany). An LCHD-05 load cell manufactured by Omega Engineering, Inc. (Norwalk, CT, USA) was employed to close the force loop. Mechanical compliance was provided by a spring. Given the fact that lower sensors were more heavily loaded than on-top sensors, the error metrics from later sections took such a difference into account; this had a negligible impact on full sensor loading. However, in regard to the null-force condition, a clarification is required. The uppermost and lowermost sensors had the null-force loading of 0.49 N and 0.96 N, respectively. In the worst case scenario, the null-force loading represented only 4.8% of FSRs’ nominal capacity rated at 20 N; therefore, we could state that the sandwich-like configuration from Fig. 1 was a valid setup to speed up the characterization process with little effect on the performance metrics.

![Fig. 1. Test bench for handling up to sixteen sensors simultaneously. (A) Overview of the testbench, the forces were applied with the linear motor (i) on-top of the arrangement, and the force loop was closed using the load cell (ii). The temperature chamber (iii) provided mechanical support to the structure and held temperature constant at 25°C along the tests. Bunch of commercial Force Sensing Resistors (FSRs) (iv). (B) Close-up view of the linear motor and the load cell. (C) Sandwich-like configuration for handling the sensors, the spring (v) provided mechanical compliance to the arrangement of FSRs (vi).](image-url)
The control scheme of the testbench is summarized in Fig. 2 (top). A digital Proportional Integral controller, $PI(z)$, was implemented to match the reference force ($F_r$) with the force measured at the bunch of sensors ($F_o$). The $PI(z)$ was implemented in LabVIEW using a cRIO-9035 Real-Time embedded controller. It must be emphasized that $PI(z)$ was tuned to avoid overshoot; this was required because FSRs exhibit considerable amounts of hysteresis that causes a non-linear variation in their output. Given the resolution of the stepper motor and the spring constant, the minimal force increment was set to 10 mN with a bandwidth of roughly 2 Hz; this frequency bandwidth was more than enough to apply the force profiles of the experimental characterization. In fact, the system bandwidth was limited to 1 Hz by the analog multiplexer circuit of Fig. 3, and not by mechanical constraints of the testbench.

According to the sensors’ datasheet, the Interlink FSR 402 and the Peratech SP200-10 sensors have the nominal capacities of 20 N [26, 27]. Both sensors have a continuous output meaning that a small increment in force and/or input voltage causes a variation in sensor’s resistance; this has been demonstrated by our previous studies [28] and by third authors as well [23, 29]. The continuous output of both FSRs implies that sensors’ sensitivity and performance metrics
are influenced by the input voltage. Therefore, we require a driving circuit that lets us control the voltage across the sensors at any time; this can be achieved by means of an amplifier in inverting configuration, see Fig. 3. The low noise amplifier model OP470 was chosen for this purpose.

In order to enable readings from multiple sensors, a time-multiplexed circuit was implemented on the basis of the analog multiplexer model ADG444, see Fig. 3. A total of four ADG444 were incorporated, each with four analog inputs, thus enabling us to handle up to sixteen FSRs. Given the low on-resistance of the multiplexer (around 70 Ω), the error introduced by the mux could be neglected. A feedback resistor (\(R_f\)) of 510 Ω was chosen for all the tests with a tolerance of 1%. Given the input voltage (\(U_s\)), each sensor was activated accordingly to be sourced with \(U_s\), and mechanically loaded with the intended force profile, i.e., with \(F_r\) in Fig. 2.

Three different force profiles were explored to assess the sensors’ sensitivity and the performance metrics of hysteresis and drift; the protocols are next described:

### 2.1. Sensitivity characterization and general considerations

The bunch of sensors were loaded in step increments of 1 N starting at null-input force up to the sensors’ nominal range at 20 N. Later, we performed regression analysis to obtain the sensitivity of each sensor. The amplifier output voltage (\(U_o\)) was set as the system output, thanks to which we obtained a linear relationship between the applied force and \(U_o\); this has been previously reported in literature [22, 23]. This procedure was repeated at the following input voltages, \(U_s\): 0.25 V, 0.5 V, 0.75 V, 1 V. For voltages larger than 1 V, step increments of 0.5 V were applied up to 8.5 V. Therefore, a total of 19 different voltages were applied to the 48 specimens of each sensor brand.

The piezoresistive response of FSRs originates from two different phenomena: quantum tunnelling occurring in neighbouring particles, and constriction resistance occurring in particles in contact. This model was derived by Kalantari et al. [30] and was also demonstrated by the authors [31]. Both quantum tunnelling and constriction resistances are reduced for incremental forces, however, the former is heavily influenced by the input voltage [32], whereas the latter is not [33]. This has the ultimate consequence i.e. performance metrics are influenced by \(U_s\). For this reason, we performed the sensors’ characterization at multiple voltages.

### 2.2. Hysteresis characterization

In order to determine the hysteresis error (\(HE\)), the following force profile was applied to the bunch of sensors: null-input force, half-nominal range (\(U_o\_loading\)(10 N)), full sensor loading (\(U_o\)(20 N)), and then back to the half-nominal range (\(U_o\_unloading\)(10 N)); this procedure was repeated at the input voltages specified in Section 2.1 for all the sensors. Finally, the Hysteresis Error (\(HE\)) was computed at each \(U_s\) from the following formula:

\[
HE(\%) = \frac{U_o\_unloading (10 \text{ N}) - U_o\_loading (10 \text{ N})}{U_o (20 \text{ N})} \cdot 100\%.
\]

### 2.3. Drift characterization

Drift error originates from viscoelastic response of polymers. In order to determine the drift error, the sensors were loaded to a constant force of 15 N for a time span of one hour. Immediately after the application of the force, \(U_o\) was registered for all sensors; this measurement
was designated as $U_o(0\, \text{h})$. After one hour, the output voltage was registered again to obtain $U_o(1\, \text{h})$. With these data, the Drift Error ($DE$) was computed on the percentage basis as follows:

$$DE(\%) = \frac{U_o(1\, \text{h}) - U_o(0\, \text{h})}{U_o(0\, \text{h})} \cdot 100\%.$$ (2)

The aforementioned procedure was repeated at all the input voltages specified in this Section. This let us assess the drift error as a function of $U_s$.

3. Experimental results and discussion

This section discusses the experimental assessment of sensors’ sensitivity, hysteresis and drift errors at multiple input voltages, $U_s$. Dispersion analysis is embraced for each metric on the basis of the $\mu/\sigma$ quotient where $\mu$ and $\sigma$ are respectively the mean value of the metric and its standard deviation. The rule of thumb when comparing sensors is that the error metric should be as low as possible, and also, dispersion should be held to a minimum. Low dispersion implies a high $\mu/\sigma$ that ultimately yields high part-to-part repeatability.

3.1. Sensitivity results

Figure 4 shows the sensitivity dispersion for the whole set of input voltages and for both sensor brands. In general, there is not a remarkable difference in the dispersion of both brands, but noticeably, the sensitivity dispersion of Interlink sensors exhibits less variation to changes in the input voltage. On the hand, the sensitivity dispersion of Peratech sensors shows jitter when the input voltage is changed. To better understand the jitter phenomenon, we plotted in Fig. 5 sensor sensitivity as a function of $U_s$ for individual sensors. Note that sensitivity increases in a smooth way for the Interlink sensors. This results in a rather invariant $\mu/\sigma$ quotient in Fig. 4. Conversely, some Peratech sensors show step increments in sensitivity for $U_s$ within the range of 5 V to 7 V, (see the arrow marks in the plot). This, in turn, results in a jitter-like response to the dispersion ratio of Fig. 4. The practical implications of jitter are discussed later.

![Fig. 4. Dispersion in the sensors’ sensitivity as a function of input voltage ($U_s$). Dispersion calculated from the $\mu/\sigma$ quotient.](image-url)
On the other hand, the fanning out of sensitivities with incremental $U_s$ may be initially understood as a widening of the sensors’ differences with larger input voltages. This observation holds for both sensor brands plotted in Fig. 5. However, by recalling the results of Fig. 4, the following statement can be done: when $U_s$ is increased, the absolute difference in individual sensitivities is enlarged, but on a relative basis the dispersion is held constant. This is so because the standard deviation grows in the same proportion as the mean. From this observation, we can claim that there is not an optimal voltage that minimizes dispersion in sensitivity for the Interlink sensors. Conversely, when Peratech sensors are sourced with 6 V, there is a maximum in the $\mu/\sigma$ ratio. In practice, this implies that lowest measured dispersion occurs at 6 V, and ultimately, part-to-part repeatability is enhanced.

The underlying phenomena for the jitter behaviour are manifold, but providing an explanation for them falls out of the scope for this article. From the plots in Fig. 5, we can state that this is not an isolated phenomenon as many sensors exhibited the same response.

Fig. 5. Sensors’ sensitivity as a function of input voltage ($U_s$) for both sensor brands. Left: Interlink FSR402. Right: Peratech SP200-10. The arrows indicate the step increments in sensitivity for $U_s$ in the range of 5 V to 7 V.

3.2. Hysteresis error results

The hysteresis error of both sensor brands is shown in Fig. 6; the dispersion in the hysteresis error is shown as well. It is clear from Fig. 6 that the Interlink sensors exhibit a lower hysteresis error for any input voltage. Likewise, it is interesting to note that the $HE$ is a voltage-dependent phenomenon as theoretically deducted in a previous work by the authors [31]. From the standpoint of dispersion, it can be noticed from Fig. 6 that the relative dispersion is slightly higher for the Interlink sensor, i.e. lower $\mu/\sigma$ means higher dispersion. From a different standpoint, the Peratech sensor exhibits a higher $HE$, but a slightly larger part-to-part repeatability regarding this error metric.

Finally, from the standpoint of the $HE$, there is not a clear best pick, since low error metric and low dispersion are split among both brands. Modelling and compensation of the $HE$ is especially useful when dealing with cyclic forces in certain applications, such as gait analysis [34] and footwear design [35].
3.3. Drift error results

The drift error and its dispersion are shown in Fig. 7 for both sensor brands. In this case, the Peratech sensors exhibit a lower DE than the Interlink sensors, but a relative higher dispersion. In other words, the electrical resistance of an Interlink sensor drifts more over time when compared with a Peratech sensor, but in general, Interlink sensors exhibit more repeatable drift readings. The practical consequences of the results reported in Fig. 7 are discussed in the next section.

Drift is the major drawback of FSRs that it is currently limiting their extensive usage. Certain implementations that involve application of force over an extended time period require low
drift readings that FSRs cannot currently meet. Previous work of the authors had focused on deep understanding of the drift phenomenon of FSRs. It was then found that drift is a voltage-dependent phenomenon [28]. In brief, the larger $U_s$ is, the lower the $DE$ results, and therefore, it is advisable to source the FSRs at a high $U_s$ in order to reduce the $DE$. Note that this observation also applies to the $HE$ as previously reported in the plot of Fig. 6. However, there is a limit on how big $U_s$ can be without affecting FSRs performance. If $U_s$ is over 7 V, sensors’ sensitivity degrades over time [31].

3.4. Discussion of results

In order to provide a meaningful discussion of the experimental results, we must bear in mind two aspects: first, what is the intended final application of the FSRs? And second, what is more important in our final application, the error metric or the part-to-part repeatability?

As previously mentioned, applications with cyclic loading such as gait analysis [34] and footwear design [35], require sensors with the lowest possible hysteresis error. Typically, this kind of applications demands multiple sensors, and therefore, part-to-part repeatability is also desirable. However, poor part-to-part repeatability can be overcome with individual sensor calibration, but this clearly requires additional time and effort that ultimately translates into higher costs.

On the other hand, certain applications incorporate FSRs to distinguish objects by their force profile [36], thus requiring multiple FSRs [37]. In this final application, error metrics of hysteresis and drift are less important, but part-to-part repeatability is clearly more relevant.

A different type of application incorporates FSRs as means of estimating the amount of items in an inventory system [38]. Considering that inventory management requires a continuous measuring over an extended time period, drift error plays a major role in this scenario. However, part-to-part repeatability should be also taken into account because this type of deployment requires multiple sensors, and also, the inventory system must be replicated for every item in the store.

In order to address the initial questions from this section, we must decide whether individual sensor calibration is available or not. If available, metric dispersion is less important, and therefore, a low error metric is the most important factor for picking one brand over another. In this scenario, we may skip error compensation depending on the final application requirements. Conversely, if individual sensor calibration is not possible, it is advisable to pick the sensor model with the lowest dispersion in the error metric of interest, and then provide error compensation via software using global parameters. The definition of global parameters implies that we compensate for a given error on the basis of an average, e.g., we obtain an average drift error for multiple sensors of a specific brand, and then perform compensation with such information.

4. Conclusions

An automated testbench for characterization of FSRs has been presented. A sandwich-like configuration was employed to handle up to sixteen sensors simultaneously. Similarly, a linear motor with a spring was deployed to apply multiple force profiles to the bunch of sensors. Data collection was possible from a time-multiplexed circuit.

Experimental characterization of sensitivity, hysteresis error and drift error was carried out at multiple input voltages ($U_s$) for multiple Interlink FSR402 and Peratech SP200-10 sensors. Dispersion in these metrics was assessed by means of the quotient between the mean and the standard deviation. In regard to sensitivity, it was found that the Interlink sensor had rather con-
stant sensitivity dispersion for any input voltage, whereas the Peratech sensor exhibited minimal
dispersion at $U_s = 6$ V. Hence; we claim that $U_s = 6$ V is the optimal voltage to maximize
part-to-part repeatability in Peratech sensors.

In regard to the hysteresis and drift errors; mixed results were found. The interlink sensors
exhibited lower hysteresis error but a comparatively higher dispersion in this metric. On the other
hand, the Peratech sensors exhibited lower drift error but a comparatively higher dispersion in this
metric. Therefore, there is not the best pick sensor based on these error metrics. Every application
must evaluate the pro and cons of using either one brand or another.

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References

carbon nanocomposite wide band strain sensor. IEEE Access, 9, 14752–14764. https://doi.org/10.1109/
ACCESS.2020.3049081

structured tough conductive gel fibres for stable and high-performance wearable strain sensors. Journal

conductive hydrogels for flexible wearable sensors and energy devices: materials, structures, and

system applicable for hyperbaric environment and its application in coal and gas outburst simulation

polymerized polypyrrole–styrene–ethylene–butylene–styrene hybrid scaffold as ammonia and strain
sensor. RSC Advances, 10(38), 22533–22541. https://doi.org/10.1039/d0ra03592k

66 nanocomposite sensor for ECG, strain, temperature and gas measurements. Chemical Engineering

s10118-021-2553-8

ments in conducting polymer nanocomposites for multifunctional applications. Polymers, 13(17),
2898. https://doi.org/10.3390/polym13172898


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